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A right Choice for the Real Aspirant ICON Central Office – Madhapur – Hyderabad Jee-Main_Final_24-Feb-2021_Shift-01

PHYSICS

Max Marks: 100

(SINGLE CORRECT ANSWER TYPE)

This section contains 20 multiple choice questions. Each question has 4 options (1), (2), (3) and (4) for its answer, out of which ONLY ONE option can be correct. Marking scheme: +4 for correct answer, 0 if not attempted and –1 in all other cases.

1. In the given figure, the energy levels of hydrogen atom have been shown along with

some transitions marked A, B, C, D and E. The transitions A, B and C respectively

represent :



1) The first member of the Lyman series, third member of Balmer series and second member of Paschen series.

2) The series limit of Lyman series, second member of Balmer series and second member of Paschen series.

3) The ionization potential of hydrogen, second member of Balmer series and third member of Paschen series

4) The series limit of Lyman series, third member of Balmer series and second member of Paschen series

Key: 4

Sol: $A \rightarrow$ Series limit of laymen

 $B \rightarrow 3^{rd}$ line of Balmer

 $C \rightarrow 2^{nd}$ line of paschan

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2. A cube of side 'a' has point charges +Q located at each of its vertices except at the origin where the charge is -Q. The field at the centre of cube is :



Key: 2

- Sol: If we consider two point charges +q and -q at position of -q charge, then after interchanging -q charge with +q charge, net electric field at centre of cube is zero due to symmetry. Now remaining charges are -2q so net electric field at centre is $\left(\frac{-8kq}{2r^2}\right)$.
- 3. A current through a wire depends on time as $i = \alpha_0 t + \beta t^2$ where $\alpha_0 = 20A / s$ and $\beta = 8As^{-2}$. Find the charge crossed through a section of the wire in 15 s.

1) 2100 C2) 2250 C3) 260 C4) 11250 C

Key: 4

Sol: $\frac{dq}{dt} = (20t + 8t^2)$ $\int dq = \int_0^{15} (20t + 8t^2) dt$ $\Delta q = \left[20\frac{t^2}{2} + \frac{8t^3}{3} \right]_0^{15}$ $= \frac{20 \times (15)^2}{2} + \frac{8 \times (15)^3}{3} \quad \Delta q = 11250C$

- 4. Consider two satellites S_1 and S_2 with periods of revolution 1 hr. and 8 hr respectively revolving around a planet in circular orbits. The ratio of angular velocity of satellite S_1 to be
 - **1**) 2 : 1 **2**) 1 : 8 **3**) 1 : 4 **4**) 8 : 1

Key: 1

Sol: ratio of time period

$\frac{\mathrm{T}_{1}}{\mathrm{T}_{2}} = \frac{1}{8}$	
$\frac{\frac{2\pi}{\omega_1}}{\frac{2\pi}{\omega_2}} = \frac{1}{8}$	$\frac{\omega_1}{\omega_2} = 8$

5. Match List I with List II.

List I

List II

a) Isothermal	i) Pressure constant
b) Isochoric	ii) Temperature constant
c) Adiabatic	iii) Volume constant
d) Isobaric	iv) Heat content is constant

Choose the correct answer from the options given below :

1)
$$(a) \rightarrow (ii), (b) \rightarrow (iv), (c) \rightarrow (iii), (d) \rightarrow (i)$$

2) $(a) \rightarrow (iii), (b) \rightarrow (ii), (c) \rightarrow (i), (d) \rightarrow (iv)$
3) $(a) \rightarrow (i), (b) \rightarrow (iii), (c) \rightarrow (ii), (d) \rightarrow (iv)$
4) $(a) \rightarrow (ii), (b) \rightarrow (iii), (c) \rightarrow (iv), (d) \rightarrow (i)$

Key: 4

Sol: P-iv ; Q-iii ; R-ii ; S-i

6. Given below are two statements :

Statement I : Two photons having equal linear momenta have equal wavelengths.

Statement II : If the wavelength of photon is decreased, then the momentum and energy of a photon will also decrease.

In the light of the above statements, choose the correct answer from the options given below

- 1) Both Statement I and Statement II are false
- 2) Statement I is false but Statement II is true
- 3) Both Statement I and Statement II are true
- 4) Statement I is true but Statement II is false

Key: 4

- **Sol:** $\lambda = \frac{h}{p}$
- 7. If the velocity time graph has the shape AMB, what would be the shape of the corresponding acceleration-time graph?



Key: 1

Sol: v = -mt + C

$$\frac{dv}{dt} = -m$$
$$|v = mt - C$$
$$\frac{dv}{dt} = m$$

8. In a Young's double slit experiment, the width of the one of the slit is three times the other slit. The amplitude of the light coming from a slit is proportional to the slit width. Find the ratio of the maximum to the minimum intensity in the interference pattern

Sol:
$$\frac{A_1}{A_2} = \frac{1}{3}$$
 $A_1 = x, A_2 = 3x$

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$$\frac{I_{\max}}{I_{\min}} = \left(\frac{\left(A_1 + A_2\right)^2}{\left(A_1 - A_2\right)^2}\right) = \frac{\left(4x\right)^2}{\left(2x\right)^2} = \frac{16}{4} = 4:1$$

9. Each side of a box made of metal sheet in cubic shape is 'a' room temperature 'T', the coefficient of linear expansion of the metal sheet is 'a'. The metal sheet is heated uniformly, by a small temperature ΔT , so that its temperature is $T + \Delta T$. Calculate the increase in the volume of the metal box.

1)
$$\frac{4}{3}\pi a^3 \alpha \Delta T$$
 2) $3a^3 \alpha \Delta T$ **3**) $4\pi a^3 \alpha \Delta T$ **4**) $4a^3 \alpha \Delta T$

Key: 2

Sol:
$$\frac{\Delta V}{V} = \gamma \Delta T$$

= $3\alpha \Delta T$ $\Delta V = 3a^3 \alpha \Delta T$

10. In the given figure, a mass M is attached to a horizontal spring which is fixed on one side to a rigid support. The spring constant of the spring is k. The mass oscillates on a frictionless surface with time period T and amplitude A. When the mass is in equilibrium position, as shown in the figure, another mass m is gently fixed upon it. The new amplitude of oscillation will be :



Key: 2

Sol: Velocity at mean position is $= A\omega$

Conserving momentum $MA\omega_0 = (M + m)V^1$

$$V^{1} = \frac{MA\omega_{0}}{M+m} = (A')\sqrt{\frac{K}{M+m}} \qquad A' = \frac{MA\sqrt{\frac{K}{M}}}{M+m} \times \sqrt{\frac{M+m}{K}} = \sqrt{\frac{M}{(M+m)}}A$$

- 11. The work done by a gas molecule in an isolated system is given by, $W = \alpha \beta^2 e \frac{X^2}{\alpha KT}$, where x is the displacement k is the Boltzmann constant and T is the temperature, α and
 - β are constants. Then the dimensions of β will be :
 - **1**) $\begin{bmatrix} M^0 L T^0 \end{bmatrix}$ **2**) $\begin{bmatrix} M^2 L T^2 \end{bmatrix}$ **3**) $\begin{bmatrix} M L T^{-2} \end{bmatrix}$ **4**) $\begin{bmatrix} M L^2 T^{-2} \end{bmatrix}$

Key: 3

Sol:
$$\frac{x^2}{\alpha KT}$$
 = dimensions
 $\frac{L^2}{KT} \Rightarrow \alpha$
 $\alpha \Rightarrow \frac{L^2}{v^2 M} = L^2 M^{-1} L^{-2} T^2 = M^{-1} T^2$
work = $\alpha . \beta^2$. (dimensionless)
 $M^1 L^1 T^{-2} . L^1 = M^{-1} T^2 \beta^2$
 $v = \sqrt{\frac{3KT}{M}}$
 $\frac{v^2 . M}{3} = KT$
 $\beta = M^1 L T^{-2}$

12. The focal length f is related to the radius of curvature r of the spherical convex mirror by:

1)
$$f = -\frac{1}{2}r$$
 2) $f = +\frac{1}{2}r$ **3**) $f = r$ **4**) $f = -r$

Key: 2

Sol: $\frac{R}{2} = f$

13. n mole of a perfect gas and undergoes a cyclic process ABCA (see figure) consisting of the following processes.

 $A \rightarrow B$: Isothermal expansion at temperature T so that the volume is doubled from V_1 to $V_2 = 2V_1$ and pressure changes from P_1 to P_2 .

 $B \rightarrow C$: Isobaric compression at pressure P_2 to initial volume V_1



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Sri Chaitanya IIT Academy, India.Final_Jee-Main_24-Feb-2021_ $C \rightarrow A$: Isochoric change leading to change of pressure from P_2 to P_1 .

Total work done in the complete cycle ABCA is :



$$W_{BC} = -P_1 V_1$$
$$W_{CA} = 0$$
$$W_{ABCA} = (2P_1 V_1 \ell n 2 - P_1 V_1)$$
$$= nRT(2\ell n 2 - 1)$$

If Y, K and η are the values of Young's modulus, bulk and modulus of rigidly of any 14. material respectively. Choose the correct relation for those parameters.

1)
$$Y = \frac{9K\eta}{2\eta + 3K} N / m^2$$

2) $\eta = \frac{3YK}{9K + Y} N / m^2$
3) $K = \frac{Y\eta}{9\eta - 3Y} N / m^2$
4) $Y = \frac{9K\eta}{3K - \eta} N / m^2$

Key: 3

Sol:

15. Moment of inertia (M.I.) of four bodies, having same mass and radius, are reported as; $I_1 = M.I.$ of thin circular ring about its diameter,

 $I_2 = M.I.$ of circular disc about an axis perpendicular to disc and going through the centre.

 $I_3 = M.I$ of solid cylinder about its axis and

 $I_4 = M.I.$ of solid sphere about its diameter.

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1) $I_1 + I_3 < I_2 + I_4$	2) $I_1 + I_2 = I_3 + \frac{5}{2}I_4$
3) $I_1 + I_2 = I_3 < I_4$	4) $I_1 = I_2 = I_3 > I_4$
Key: 4	
$Sol: I_1 = \frac{MR^2}{2}$	
$I_2 = \frac{MR^2}{2}$	
$I_3 = \frac{MR^2}{2}$	
$I_4 = \frac{2}{5}MR^2$	

16. Two equal capacitors are first connected in series and then in parallel. The ratio of the equivalent capacities in the two cases will be:

1) 2 : 1 **2**) 1 : 2 **3**) 4 : 1 **4**) 1 : 4

Key: 4

Sol:



$$\frac{\mathrm{C}_1}{\mathrm{C}_2} = \frac{1}{4}$$

17. Four identical particles of equal masses 1 kg made to move along the circumference of a circle of radius 1 m under the action of their own mutual gravitational attraction. The speed of each particle will be :

1)
$$\sqrt{G(1+2\sqrt{2})}$$
 2) $\frac{\sqrt{(1+2\sqrt{2})G}}{2}$ **3**) $\sqrt{\frac{G}{2}(2\sqrt{2}-1)}$ **4**) $\sqrt{\frac{G}{2}(1+2\sqrt{2})}$



Sol:

Net force on one particle $F_{net} = F_1 + 2F_2 \cos 45^\circ =$ centripetal force

$$\Rightarrow \frac{GM^2}{(2R)^2} + \left[\frac{2GM^2}{(\sqrt{2}R)^2}\cos 45^\circ\right] = \frac{MV^2}{R}$$
$$V = \frac{1}{2}\sqrt{\frac{GM}{R}(1+2\sqrt{2})}V = \frac{1}{2}\sqrt{G(1+2\sqrt{2})}V$$

A cell E_1 of emf 6V and internal resistance 2Ω is connected with another cell E_2 of emf 18. 4 V and internal resistance 8Ω (as shown in the figure). The potential difference across points X and Y is :

1) 10.0 V **2**) 3.6 V

3) 5.6 V

4) 2.0 V

Key: 3

Sol: Current I = $\frac{6-4}{10} = \frac{1}{5}A$ $\begin{array}{c|c} E_1 & \chi & E_2 & Y \\ \hline & & & & \\ 6 & V, 2 & \Omega & 4 & V, 8 & \Omega \end{array}$ $v_x + 4 + 8 \times \frac{1}{5} = v_y$ $v_{x} + v_{y} = -5.6v$

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19.	If an emitter current is changed by 4 mA, the collector current changes by 3.5 mA. Th			y 3.5 mA. The	
	value of β will be :				
	1) 0.875	2) 3.5	3) 7	4) 0.5	
Key:	Key: 3				
Sol:	$\Delta I_{\rm E} = 4$				
	$\Delta I_{\rm C} = 3.5$				
	$\alpha = \frac{\Delta I_{\rm C}}{\Delta I_{\rm E}} = \left(\frac{\Delta I_{\rm C}}{\Delta I_{\rm E}}\right)$	$\left(\frac{3.5}{4}\right) = \left(\frac{7}{8}\right)$			

$$\beta = \frac{\alpha}{1 - \alpha} = \frac{\frac{7}{8}}{1 - \frac{7}{8}} = 7$$

20. Two stars of masses m and 2m at a distance d rotate about their common centre of mass in free space. The period of revolution is:

1)
$$\frac{1}{2\pi}\sqrt{\frac{d^3}{3Gm}}$$
 2) $2\pi\sqrt{\frac{3Gm}{d^3}}$ 3) $\frac{1}{2\pi}\sqrt{\frac{3Gm}{d^3}}$ 4) $2\pi\sqrt{\frac{d^3}{3Gm}}$
Key: 4
Sol:
 $\frac{G(m)(2m)}{d^2} = m\omega^2 \times \frac{2d}{3}$
 $\frac{2Gm}{d^2} = \omega^2 \times \frac{2d}{3}$
 $\omega^2 = \frac{3Gm}{d^3}$ $\omega = \sqrt{\frac{3Gm}{d^3}}; T = 2\pi\sqrt{\frac{d^3}{3Gm}}$
(NUMERICAL VALUE TYPE)
This section contains 10 questions. Each question is numerical value type. For each question, enter the correct numerical value (in decimal notation, truncated/rounded-off to second decimal place. (e.g. 6.25, 7.00, 0.33, 30, 30.27, 127.30). Attempt any five questions out of 10. Marking scheme: +4 for correct answer; 0 if not attempted and 0 in all other cases.
21. A ball with a speed of 9 m/s collides with another identical ball at rest. After the

collision, the direction of each ball makes an angle of 30° with the original direction. The ratio of velocities of the balls after collision is x : y, where x is _____

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Sol: Using linear momentum conservation in y- direction $P_i = 0$

$$P_{f} = m \times \frac{1}{2}v_{1} - m \times \frac{1}{2}v_{2}$$
$$v_{1} = v_{2}$$

A common transistor radio set requires 12 V (D.C) for its operation. The D.C. source is constructed by using a transformer and a rectifier circuit, which are operated at 220V (A.C) on standard domestic A.C. supply. The number of turns of secondary coil are 24, then the number of turns of primary are ______

Key: 440

Sol:
$$\frac{N_{P}}{N_{S}} = \frac{V_{P}}{V_{S}}$$
$$\frac{N_{P}}{24} = \frac{220}{12}; N_{P} = 440$$

23. The coefficient of static friction between a wooden block of mass 0.5 kg and a vertical rough wall is 0.2. The magnitude of horizontal force that should be applied on the block to keep it adhere to the wall will be _____ N. $[g = 10 \text{ms}^{-2}]$

Key: 25

Sol:
$$F = N$$
, $f = 0.2 \times N$



 $0.2N \leq 5$

 $N \leq 25$

24. An unpolarized light beam is incident on the polarizer of a polarization experiment and the intensity of light beam emerging from the analyzer is measured as 100 Lumens. Now, if the analyzer is rotated around the horizontal axis (direction of light) by 30° in clockwise direction the intensity of emerging light will be _____Lumens.

Sol: $I = I_o \cos^2 \theta = I_o \cos^2 30^\circ = I_o \left(\frac{3}{4}\right) = 75$

25. A hydraulic press can lift 100 kg when a mass 'm' is placed on the smaller piston. It can lift ______ kg when the diameter of the larger piston is increased by 4 times and that of the smaller piston is decreased by 4 times keeping the same mass 'm' on the smaller piston.

Key: 25600

Sol: Initially
$$\frac{100g}{A_1} = \frac{mg}{A_2}$$
.....(i)
Initially $\frac{Mg}{16A_1} = \frac{mg}{\left(\frac{A_2}{16}\right)}$(ii)
 $\frac{100 \times 16}{M} = \frac{1}{16} = M = 25600 \text{kg}$

26. A resonance circuit having inductance and resistance 2×10^{-4} H and 6.28Ω respectively oscillates at 10 MHz frequency. The value of quality factor of this resonator is _____. $[\pi = 3.14]$

Key: 200

Our key is : 2000

Sol:
$$Q = \frac{x_L}{R} = \frac{\omega L}{R} = \frac{2\pi f L}{R}$$

 $Q = \frac{2\pi \times 10^6 \times 10 \times 2 \times 10^{-4}}{6.28} = 2000$
 $Q = 2000$

27. An electro magnetic wave of frequency 5 GHz is travelling in a medium whose relative electric permittivity and relative magnetic permeability both are 2. Its velocity in this medium is $\pm 10^7 \text{ m/s}$.

Sol:
$$n = \sqrt{\mu_r \varepsilon_r} = 2$$

 $v = \frac{C}{n} = \frac{3 \times 10^8}{2} = 15 \times 10^7 \, \text{m/s}$
 $x = 15$

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28. In connection with the circuit drawn below, the value of current flowing, through $2k\Omega$ resistor is _____× 10^{-4} A.



Key: 25

Sol: Zener diode breakdown

$$\Rightarrow i = \frac{5}{2 \times 10^{-3}} = 2.5 \times 10^{-3}$$
$$x \times 10^{-4} = 2.5 \times 10^{-3}$$
$$x = 2.5 \text{mA}$$

29. An inclined plane is bent in such a way that the vertical cross-section is given by $y - \frac{x^2}{4}$ where y is in vertical and x in horizontal direction. If the upper surface of this curved plane is rough with coefficient of friction $\mu = 0.5$, the maximum height in cm at which a stationary block will not slip downward is _____cm.

Key: 25

Sol:
$$\mu \ge \tan \theta = \frac{dy}{dx} = \frac{dx}{4} = \frac{x}{2}$$

 $0.5 \ge \frac{x}{2}$ $x \le 1$
 $\sqrt{4y \le 1}$
 $2\sqrt{y} \le 1$
 $y \le \frac{1}{4}$

30. An audio signal $v_m = 20 \sin 2\pi (1500t)$ amplitude modulates a carrier $v_c = 80 \sin 2\pi (100,000t)$.

The value of percent modulation is _____

Sol: m% =
$$\frac{A_m}{A_c} \times 100 = \frac{20}{80} \times 100 = 25\%$$

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CHEMISTRY

(SINGLE CORRECT ANSWER TYPE)

This sect	ion contains 20 multiple choice questions. Each que	stion has 4 options (1), (2), (3) and (4) for its answer, out of which ONLY ONE option can be				
Marking	g scheme: +4 for correct answer, 0 if not attempt	ed and -1 in all other cases.				
31.	Which of the following ore is c	concentrated using group 1 cyanide salt?				
	1) Calamine2) Siderite	3) Sphalerite4) Malachite				
Key:	3					
Sol:	NaCN is used as depressant in Sphalerite	froth flotation process for the separation of galena &				
32. Al_2O_3 was leached with alkali to get X. The solution of X on passing of gas Y						
	X, Y and Z respectively are :					
	1) $X = Al(OH)_3, Y = SO_2, Z = Al_2O_3.xH_2O$					
	2) $X = Na[Al(OH)_4], Y = CO_2, Z = Al_2O_3.xH_2O$					
	3) $X = Na \left[Al \left(OH \right)_4 \right], Y = SO_2, Z = Al_2O_3.xH_2O$					
	4) $X = Al(OH)_3, Y = CO_2, Z =$	Al_2O_3				
Key:	2					
Sol:	$Al + 4NaOH \longrightarrow Na(Al(OH)_4) \longrightarrow Na_2CO_3 + Al_2O_3.xH_2O$					
33.	3. Out of the following, which type of interaction for the stabilisation of α – helix stru					
	of protons ?					
	1) Covalent bonding	2) Hydrogen bonding				
	3) Ionic bonding	4) vander Waals forces				
Key:	2					
Sol:	Hydrogen bond is responsible	for the stacking of α – helix structure of protein.				
34.	Match List – I with List – II.					
	List - I	List – II				
	(Monomer Unit)	(Polymer)				
	(a) Caprolactum	(i) Natural rubber				
	(b) 2-Chloro-1, 3-butadiene	(ii) Buna – N				
	(c) Isoprene	(iii) Nylon 6				
	(d) Acrylonitrile	(iv) Neoprene				
	Choose the correct answer from	n the options given below :				
	1) $a \rightarrow i, b \rightarrow ii, c \rightarrow iii, d \rightarrow iv$	2) $a \rightarrow iv, b \rightarrow iii, c \rightarrow ii, d \rightarrow i$				
	3) $a \rightarrow ii, b \rightarrow i, c \rightarrow iv, d \rightarrow iii$	4) $a \rightarrow iii, b \rightarrow iv, c \rightarrow i, d \rightarrow ii$				

Key: 4

Sol: $a \rightarrow iii, b \rightarrow iv, c \rightarrow i, d \rightarrow ii$

35. (A)
$$HOCl + H_2O_2 \rightarrow H_3O^+ + Cl^- + O_2$$

(B)
$$I_2 + H_2O_2 + 2OH^- \rightarrow 2I^- + 2HO + O_2$$

Choose the correct option

1) H₂O₂ acts as reducing and oxidizing agent respectively in equations (A) and (B)

2) H₂O₂ acts as reducing agent in equations (A) and (B)

3) H_2O_2 acts as oxidixing agent in equations (A) and (B)

4) H₂O₂ acts as oxidixing and reducing agent respectively in equations (A) and (B)

- **Sol:** In 1 & 2 H_2O_2 acts as reducing agent
- **36.** What is the final product (major) 'A' in the given reaction ?





Key: 2



Sol:

38. Which of the following compound gives pink colour on reaction with phthalic anhydride in conc. H₂SO₄ followed by treatment with NaOH ?





Key: 1

Sol: SO₄²⁻ & CrO₄²⁻, SiCl₄ & TiCl₄ The two pairs are isostructural, all are tetrahedral
40. In Freundlich adsorption isotherm, slope of AB line is :



Sol:
$$\frac{x}{m} = kp^{1/n}$$

 $\log \frac{x}{m} = \log k + \frac{1}{n}\log p$
 $Slope = \frac{1}{n}(0to1)$

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41. The gas released during anaerobic degradation of vegetation may lead to :

1) Corrosion metals2) Ozone hole

3) Global warming and cancer 4) Acid rain

Key: 3

- **Sol:** The gas CH₄ evolved due to anaerobic degradation of vegetation which causes global warming and cancer.
- 42. The product formed in the first step of the reaction of

$$CH_{3} - CH_{2} - CH - CH_{2} - CH - CH_{3} \text{ with excess } Mg / Et_{2}O(Et = C_{2}H_{5}) \text{ is :}$$

$$Br$$

$$CH_3 - CH_2 - CH - CH_2 - CH - CH_3$$

$$|$$

$$|$$

$$CH_3 - CH_3 - CH - CH_3 - CH - CH_3$$

1)
$$CH_3 = CH_2 = CH = CH_2 = CH = CH_3$$

 $CH_2 = CH_2 = CH = CH_2 = CH = CH_2$

2)
$$CH_{2} = CH_{2} = CH_{2} = CH_{2} = CH_{3}$$





Key: 4

4)



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43. Which of the following regents is used for the following reaction ?

 $CH_{3}CH_{2}CH_{3} \xrightarrow{?} CH_{3}CH_{2}CHO$

1) Potassium permanganate

- 2) Molybdenum oxide
- 3) Manganese acetate
- 4) Copper at high temperature and pressure

Key: 2

- Sol: Control oxidizing reagent is molybdenum oxide
- **44.** Consider the elements Mg, Al, S, P ad Si, the correct increasing order of their first ionization enthalpy is :

1) Mg < Al < Si < S < P	2) Mg < Al < Si < P < S
3) Al $<$ Mg $<$ S $<$ Si $<$ P	4) Al < Mg < Si < S < P

- **Sol:** Al < Mg < Si < S < P
- **45.** Identify products A and B.









1) – NH_2 group is highly meta-directive

2) – NO₂ substitution always takes place at meta-position

3) Formation of anilinium ion

4) Low temperature

Key: 3

Sol: In acidic medium, aniline is converted into anilinium ion which is meta directing

(NUMERICAL VALUE TYPE)

This section contains 10 questions. Each question is numerical value type. For each question, enter the correct numerical value (in decimal notation, truncated/rounded-off to second decimal place. (e.g. 6.25, 7.00, 0.33, 30, 30.27, 127.30). Attempt any five questions out of 10. Marking scheme: +4 for correct answer, 0 if not attempted and 0 in all other cases.

51. 4.5 g of compound A (MW = 90) was used to make 250 mL of its aqueous solution. The molarity of the solution in M is $x \times 10^{-1}$. The value of x is _____. (Rounded off to the

nearest integer)

Key: 2

- Sol: $M = \frac{n}{V} = \frac{4.5/90}{250/1000} = 0.2 = 2 \times 10^{-1}$
- **52.** The reaction of sulphur in alkaline medium is given below :

$$S_{8(s)} + a OH_{(aq)}^{-} \rightarrow b S_{(aq)}^{2-} + c S_2 O_{3(aq)}^{2-} + dH_2 O_{(l)}$$

The value of 'a' is _____ (Integer answer)

Key: 12

- **Sol:** $S_8 + 12OH^- \longrightarrow cS^{2-} + dS_2O_3^{2-} + H_2O$
- **53.** At 1990 K and 1 atm pressure there are equal number of Cl_2 molecules and Cl atoms in the reaction mixture. The value of K_p for the reaction $Cl_{2(g)} \rightleftharpoons 2Cl_{(g)}$ under the above

conditions is $x \times 10^{-1}$. The value of x is _____ (Rounded off to the nearest integer).

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Sol: $Cl_2 \rightleftharpoons 2Cl$ Moles at equilibrium x x

$$\frac{1}{2}$$

1

 $\overline{2}$

$$K_{p} = \frac{P_{Cl}^{2}}{P_{Cl}}$$
$$= \frac{\left(\frac{1}{2}\right)^{2}}{\frac{1}{2}} = \frac{1}{2} = 0.5$$
$$= 5 \times 10^{-1} = 5$$

P.P.

54. The stepwise formation of $\left[Cu(NH_3)_4\right]^{2+}$ is given below

$$Cu^{2+} + NH_{3} \xleftarrow{K_{1}} \left[Cu(NH_{3}) \right]^{2+}$$

$$\left[Cu(NH_{3}) \right]^{2+} + NH_{3} \xleftarrow{K_{2}} \left[Cu(NH_{3})_{2} \right]^{2+}$$

$$\left[Cu(NH_{3})_{2} \right]^{2+} + NH_{3} \xleftarrow{K_{3}} \left[Cu(NH_{3})_{3} \right]^{2+}$$

$$\left[Cu(NH_{3})_{2} \right]^{2+} + NH_{3} \xleftarrow{K_{1}} \left[Cu(NH_{3})_{4} \right]^{2+}$$

The value of stability constants K_1 , K_2 , K_3 and K_4 are 10^4 , 1.58×10^3 , 5×10^2 and 10^2 respectively. The overall equilibrium constants for dissociation of $\left[Cu(NH_3)_4\right]^{2+}$ is $x \times 10^{-12}$. The value of x is _____. (Rounded off to the nearest integer).

Sol:
$$\left[Cu \left(NH_3 \right)_4 \right]^{2+} \rightleftharpoons Cu^{2+} + 4NH_3$$

 $K = \frac{1}{K_1 K_2 K_3 K_4} = \frac{1}{10^4 \times 1.58 \times 10^3 \times 5 \times 10^2 \times 10^2}$
 $= 1.26 \times 10^{-12} = 1.26$

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55. A proton and a Li^{3+} molecule are accelerated by the same potential. If λ_{Li} and λ_{p} denote

the de Broglie wavelength of Li^{3+} and proton respectively, then the value of $\frac{\lambda_{\text{Li}}}{\lambda_{p}}$ is

 $x \times 10^{-1}$. The value of x is _____. (Rounded off to the nearest integer).

[Mass of $Li^{3+} = 8.3$ mass of proton]

Key: 2

Sol: $\lambda_{DB} \alpha \frac{1}{\sqrt{m.K.E}}$ $\frac{\lambda_{Li^{3+}}}{\lambda_p} = \sqrt{\frac{m_p \times e_p V}{8.33m_p \times 3e_p V}}$ $\sqrt{\frac{1}{25}} = \frac{1}{5} = 0.2 = 2 \times 10^{-1}$

56. Number of amphoteric compounds among the following is _____

i) BeO	ii) BaO	iii) Be(OH) ₂	iv) Sr(OH) ₂
--------	---------	--------------------------	-------------------------

Key: 2

Sol: Be(OH)₂, BeO

57. For the reaction $A_{(g)} \rightarrow B_{(g)}$ the value of the equilibrium constant at 300 K and 1 atm is equal to 100.0. The value of $\Delta_r G$ for the reaction at 300 K and 1 atm in J mol⁻¹ is -xR, where x is _____. (Rounded off to the nearest integer).

$$(R = 8.31 J mol^{-1} K^{-1} and in 10 = 23)$$

Key: 1380

Sol: $\Delta_r G^{\circ} = -RT \ln K_{eq}$

 $= -R \times 300 \times 2 \times 2.3$

$$= -1380R$$

58. When 9.45 g of ClCH₂COOH is added to 500 mL of water, its freezing point drops by 0.5°C. The dissociation constant of ClCH₂COOH is $x \times 10^{-3}$. The value of x is

_____. (Rounded off to the nearest integer).

 $\left[K_{f}(H_{2}O) = 1.86K \text{ kg mol}^{-1} \right]$

Key: 7.5

Sol:
$$\Delta T_f = i \times k_f \times m$$

 $0.5 = (1 + \alpha) \times (1.86) \times \frac{9.45 \times 1000}{94.5 \times 500}$
 $0.5 = (1 + \alpha) \times 1.86 \times \frac{1}{5}$
 $(1 + \alpha) = \frac{0.5}{1.86} \alpha = 0.344$
 $= 344 \times 10^{-3}$

59. Gaseous cycobutene isomerizes to butadiene in a first order process which has a 'k' value of 3.3×10^{-4} s⁻¹ at 153°C. The time in minutes it takes for the isomerization to proceed 40% to completion at this temperature is _____. (Rounded off to the nearest integer).

Key: 26

Sol:
$$t = \frac{2.303}{K} \log \frac{100}{100 - x}$$

= $\frac{2.303}{3.3 \times 10^{-4}} \log \frac{100}{100 - 40}$
= $\frac{2.303}{3.3 \times 10^{-4}} \times 0.22$
= 1535.3 sec
= $\frac{1535.3}{60} = 25.58 = 26 \min$

60. The coordination number of an atom in a body-centered cubic structure is _____. [Assume that the lattice is made up of atoms].

Key: 8

Sol: Theory

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MATHEMATICS

Max Marks: 100

(SINGLE CORRECT ANSWER TYPE)

This section contains 20 multiple choice questions. Each question has 4 options (1), (2), (3) and (4) for its answer, out of which ONLY ONE option can be correct. Marking scheme: +4 for correct answer, 0 if not attempted and -1 in all other cases. 1.

61. The population P = P(t) at time 't' of a certain spectes follows the differential equation

$$\frac{dP}{dt} = 0.5P - 450. \text{ If } P(0) - 850, \text{ then the time at which population becomes zero is:}$$
1) $\frac{1}{2}\log_e 18$
2) $\log_e 9$
3) $\log_e 18$
4) $2\log_e 18$

Sol:

$$\frac{dP(t)}{dt} = \frac{P(t) - 900}{2}$$

$$\int_{0}^{t} \frac{dP(t)}{P(t) - 900} = \int_{0}^{t} \frac{dt}{2}$$

$$\{\ln|P(t) - 900| \int_{0}^{t} = \{\frac{t}{2}\}_{0}^{t}$$

$$\ln|P(t) - 900| - \ln|P(0) - 900| = \frac{t}{2}$$

$$\ln|P(t) - 900| - \ln 50 = \frac{t}{2}$$

$$Let at t = t_{1}, P(t) = 0 hence$$

$$\ln|P(t) - 900| - \ln 50 = \frac{t_{1}}{2}$$

$$t_{1} = 2 \ln 18$$

62. Let $f: R \to R$ be defined as f(x) = 2x - 1 and $g: R - \{1\} \to R$ be defined as

$$g(r) = \frac{x - \frac{1}{2}}{x - 1}$$

Then the composition function f(g(x)) is :

1) Both one-one and onto 2) Neither one-one nor onto

3) One-one but not onto 4) Onto but not one-one

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one-one, into

Can challenge as co domain of fog(x) is NOT given

63. If the tangent to the curve $y = x^3$ at the point $P(t, t^3)$ meets the curve again at Q, then the ordinate of the point which divides PQ internally in the ratio 1 : 2 is :

1) 0 **2**) $2t^3$ **3**) $-2t^3$ **4**) $-t^3$

Key: 3

Sol: Equation of tangent at $P(t, t^3)$

$$(y-t^{3}) = 3t^{2}(x-t)$$
 (1)

now solve the above equation with

y = x³ ____(2)
By (1) & (2)
x³ - t³=3t²(x - t)
x² + xt + t²=3t²
x² + xt - 2t²=0
(x - t) (x + 2t) = 0

$$\Rightarrow$$
 x = -2t \Rightarrow Q(-2t, -8t³)

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Ordinate of required point =
$$\frac{2t + (-8t^3)}{3} = -2t^3$$

64. The locus of the mid-point of the line segment joining the focus of the parabola $y^2 = 4ax$ to a moving point of the parabola, is another parabola whose directrix is:

1)
$$x = a$$
 2) $x = -\frac{a}{2}$ **3**) $x = 0$ **4**) $x = \frac{a}{2}$

Key: 3



Its directrix is $x - \frac{a}{2} = -\frac{a}{2} \Longrightarrow x = 0$

65. Two vertical poles are 150 m apart and the height of one is three times that of the other. If from the middle point of the line joining their feet, an observer finds the angles of elevation of their tops to be complementary, then the height of the shorter pole (in meters) is :

1) $20\sqrt{3}$ **2**) 25 **3**) 30 **4**) $25\sqrt{3}$



66. A man is walking on a straight line. The arithmetic mean of the reciprocals of the intercepts of this line on the coordinate axes is ¹/₄. Three stones A, B and C are placed at the points (1, 1), (2, 2) and (4, 4) respectively. Then which of these stones is/are on the path of the man?

1) B only2) A only3) C only4) All the three





Sri Chaitanya IIT Academy, India. Final_Jee-Main_24-Feb-2021_Shift-01_Q.Paper The function $f(x) = \frac{4x^3 - 3x^2}{6} - 2\sin x + (2x - 1)\cos x$: 67. **1**) Increases in $\left| \frac{1}{2}, \infty \right|$ 2) Increases in $\left(-\infty, \frac{1}{2}\right)$ **3**) Decreases in $\left[\frac{1}{2},\infty\right)$ **4**) Decreases in $\left(-\infty, \frac{1}{2}\right)$ Key: 1 $f'(x) = (2x-1)(x-\sin x)$ Sol: \Rightarrow f'(x) \ge 0 inx $\in \left[\frac{1}{2}, \infty\right)$ and $f'(x) \le 0$ in $x \in \left(\infty, \frac{1}{2}\right)$ A scientific committee is to be formed from 6 Indians and 8 foreigners, which includes at **68.** least 2 Indians and double the number of foreigners as Indians. Then the number of ways, the committee can be formed is: 1) 1625 2) 560 **3**) 575 4) 1050 **Key: 1** Sol: (2I, 4F) + (3I, 6F) + (4I, 8F) $= {}^{6}C_{2}{}^{8}C_{4} + {}^{6}C_{3}{}^{8}C_{6} + {}^{6}C_{4}{}^{8}C_{8}$ $= 15 \times 70 + 20 \times 28 + 15 \times 1$ = 1050 + 560 + 15 = 1625**69**. The system of linear equations 3x - 2y - kz = 102x - 4y - 2z = 6x + 2y - z = 5mis inconsistent if : **1**) $k \neq 3, m \in \mathbb{R}$ **2**) $k = 3, m \neq \frac{4}{5}$ **3**) $k \neq 3, m \neq \frac{4}{5}$ **4**) $k = 3, m = \frac{4}{5}$ Key: 2

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Sol:
$$\Delta = \begin{vmatrix} 3 & 2 & -k \\ 1 & 2 & -3 \\ 3 & -2 & 3 \\ 1 & 2 & -3 \end{vmatrix} = 0 \Rightarrow k = 3$$

$$\Delta_x = \begin{vmatrix} 10 & 2 & -3 \\ 3 & -2 & -3 \\ 5m & 2 & -3 \end{vmatrix} = 0$$

$$\Delta_y = \begin{vmatrix} 3 & 10 & -3 \\ 1 & 3 & 3 \\ 1 & 5m & -3 \end{vmatrix} = 6(7 - 10m)$$

$$\Delta_y = \begin{vmatrix} 3 & 2 & 10 \\ 1 & -2 & 3 \\ 1 & 2 & 5m \end{vmatrix} = 4(7 - 10m)$$
Hence, k = 3 and m $\neq \frac{7}{10}$
70. If $e^{(ce^2 x + co^4 x + cy6^4 x + ...x)\log_2 x}$ satisfies the equation $t^2 - 9t + 8 = 0$, then the value of
 $\frac{2 \sin x}{\sin x + \sqrt{3} \cos x} \left(0 < x < \frac{\pi}{2} \right)$ is:
1) $\frac{1}{2}$
2) $\frac{3}{2}$
3) $\sqrt{3}$
4) $2\sqrt{3}$
Key: 1
Sol: $e^{(co^{-1}0 \dots x)\ln^2} = 2^{cox^20 \dots x^6} (0 < x < \frac{\pi}{2})$ is:
 $2^{cox^20} = 1,8 \Rightarrow \cot^2 0 = 0,3$
 $0 < 0 < \frac{\pi}{2} \Rightarrow \cot 0 = \sqrt{3}$
 $\Rightarrow \frac{2 \sin \theta}{\sin \theta + \sqrt{3} \sin \theta} = \frac{2}{1 + \sqrt{3} \cot \theta} = \frac{2}{4} = \frac{1}{2}$
71. Let p and q be two positive numbers such that p + q = 2 and p^4 + q^4 = 272. Then p and q are roots of the equation:
1) $x^2 - 2x + 8 = 0$ 2) $x^2 - 2x + 16 = 0$ 3) $x^2 - 2x + 2 = 0$ 4) $x^2 - 2x + 136 = 0$

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Key:2
Sol:
$$(p^2 + q^2)^2 - 2p^2q^2 = 272$$

 $((p^2 + q^2)^2 - 2pq)^2 - 2p^2q^2 = 272$
 $16 - 16pq + 2p^2q^2 = 272$
 $(pq)^2 - 8pq - 128 = 0$
 $pq = \frac{8 \pm 24}{2} = 16, -8$
 $pq = 16$

The area (in sq. units) of the part of the circle $x^2 + y^2 = 36$, which is outside the parabola 72. $y^2 = 9x$, is: **1**) $24\pi + 3\sqrt{3}$ **2**) $12\pi + 3\sqrt{3}$ **3**) $12\pi - 3\sqrt{3}$ **4**) $24\pi - 3\sqrt{3}$

Key: 4

Sol: The curves intersect at points $(3, \pm 3\sqrt{3})$



Required area

$$= \pi r^{2} - 2 \left[\int_{0}^{3} \sqrt{9x} dx + \int_{3}^{6} \sqrt{36 - x^{2}} dx \right]$$
$$= 36\pi - 12\sqrt{3} - 2 \left| \frac{x}{2}\sqrt{36 - x^{2}} + 18\sin^{-1}\left(\frac{x}{6}\right) \right|_{3}^{6}$$
$$= 36p - 12\sqrt{3} - 2 \left(9\pi - \left(\frac{9\sqrt{3}}{2} + 3\pi\right) \right) = 24\pi - 3\sqrt{3}$$

73. If $f: R \to R$ is a function defined by $f(x) = [x-1]\cos(\frac{2x-1}{2})\pi$, where [.] denotes the

greatest integer function, then f is :

1) Discontinuous at all integral values of x except at x = 1

- **2**) Continuous only at x = 1
- **3**) Continuous for every real *x*
- **4**) Discontinuous only at x = 1

Key: 3

Sol: Doubtful points are $x = n, n \in I$

L.H.L =
$$\lim_{x \to n^{-}} [x-1] \cos\left(\frac{2x-1}{2}\right) \pi = (n-2) \cos\left(\frac{2x-1}{2}\right) \pi = 0$$

R.H.L = $\lim_{x \to n^{-}} [x-1] \cos\left(\frac{2x-1}{2}\right) \pi = (n-1) \cos\left(\frac{2x-1}{2}\right) \pi = 0$

f(n) = 0

Hence continuous

74. The distance of the point (1, 1, 9) from the point of intersection of the line

$$\frac{x-3}{1} = \frac{y-4}{2} = \frac{z+5}{2}$$
 and the plane x + y + z - 17 is:
1) $2\sqrt{19}$ 2) $\sqrt{38}$ 3) 38 4) $19\sqrt{2}$

Key: 2

Sol:
$$\frac{x-3}{1} = \frac{y-4}{2} = \frac{z-5}{2} = \lambda$$
$$\Rightarrow x = \lambda + 3, y = 2\lambda + 4, z = 2\lambda + 5$$

Which lies on given plane hence

$$\Rightarrow \lambda + 3 + 2\lambda + 4 + 2\lambda + 5 = 17$$
$$\Rightarrow \lambda = \frac{5}{5} = 1$$

Hence, point of intersection is Q (4, 6, 7)

 \therefore Required distance = PQ

$$=\sqrt{9+25+4}=\sqrt{38}$$

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75. An ordinary dice is rolled for a certain number of times. If the probability of getting an odd number 2 times is equal to the probability of getting an even number 3 times, then the probability of getting an odd number for odd number of times is:

1)
$$\frac{1}{32}$$
 2) $\frac{3}{16}$ **3**) $\frac{1}{2}$ **4**) $\frac{5}{16}$

Key: 3

Sol: P(odd no. twice) = P(even no. thrice)

$$\Rightarrow {}^{n}C_{2}\left(\frac{1}{2}\right)^{n} = {}^{n}C_{3}\left(\frac{1}{2}\right)^{n} \Rightarrow n = 5$$

success is getting an odd number then P(odd successes) = P(1) + P(3) + P(5)

$$= {}^{5}C_{1}\left(\frac{1}{2}\right)^{5} + {}^{5}C_{3}\left(\frac{1}{2}\right)^{5} + {}^{5}C_{5}\left(\frac{1}{2}\right)^{5}$$
$$= \frac{16}{2^{5}} = \frac{1}{2}$$

- **76.** The statement among the following that is a tautology is:
 - 1) $[A \land (A \rightarrow B)] \rightarrow B$ 2) $A \land (A \lor B)$ 3) $A \lor (A \land B)$ 4) $B \rightarrow [A \land (A \rightarrow B)]$

Key: 1

Sol:
$$A \land (\sim A \lor B) \rightarrow B$$

= $[(A \land \sim A) \lor (A \land B)] \rightarrow B$
= $(A \land B) \rightarrow B$
= $\sim A \lor \sim B \lor B$

77. The equation of the plane passing through the point (1, 2, -3) and perpendicular to the planes 3x + y - 2z = 5 and 2x - 5y - z = 7, is :

1)
$$6x - 5y + 2z + 10 = 0$$

2) $3x - 10y - 2z + 11 = 0$

3)
$$11x + y + 17z + 38 = 0$$
 4) $6x - 5y - 2z - 2 = 0$

Key: 3

Sol: Normal vector of required plane is $\vec{n} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 3 & 1 & -2 \\ 2 & -5 & -1 \end{vmatrix} = -11\hat{i} - \hat{j} - 17\hat{k}$

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$$\therefore$$
 +11 (x - 1) + (y - 2) + 17 (x + 3) = 0
 11x + y + 17z + 38 = 0

 78. If $\int \frac{\cos x - \sin x}{\sqrt{8} - \sin 2x} dx = a \sin^{-1} \left(\frac{\sin x + \cos x}{b} \right) + c$, where c is a constant of integration, then the ordered pair (a, b) is equal to :
 1) (1, -3)

 10. (1, -3)
 2) (-1, 3)
 3) (3, 1)
 4) (1, 3)

 Key:4 Sol: Put sin 0 + cos 0 = t \Rightarrow 1 + sin 20 = t²
 \Rightarrow (cos 0 - sin 0) d0 = dt
 \therefore I = $\int \frac{dt}{\sqrt{8 - (t^2 - 1)}} = \int \frac{dt}{\sqrt{9 - t^2}} = \sin^{-1} \left(\frac{1}{3} \right) + C = \sin^{-1} \left(\frac{\sin \theta + \cos \theta}{3} \right) + C$
 \Rightarrow a = 1& b = 3
 79. $\lim_{x \to 0} \frac{\int_{-1}^{0} \frac{\sin \sqrt{t}}{x^2}}{x^2}$ is equal to :
 1) $\frac{3}{2}$
2) 0
 3) $\frac{1}{15}$
4) $\frac{2}{3}$
Key: 4 Sol: $\lim_{x \to 0} \frac{\int_{-1}^{0} \sqrt{t} dt}{x^2} = \lim_{x \to 0} \left(\frac{\sin |x| 2x}{3x^2} \right) = \lim_{x \to 0} \left(\frac{\sin x}{x} \right) \times \frac{2}{3} = \frac{2}{3}$
80. The value of $-1^{15}C_{1} + 2^{15}C_{2} - 3^{15}C_{3} + \dots -15^{15}C_{15} + {}^{14}C_{1} + {}^{14}C_{3} + {}^{14}C_{1} + \lim_{x \to 0} 1 + \frac{1}{2}C_{1}$
3) $2^{13} - 13$
4) $2^{16} - 1$
Sol: $S_{1} = -1^{15}C_{1} + 2^{15}C_{2} - \dots -15^{15}C_{15} = \sum_{x=1}^{15} (-1)^{1} x^{16}C_{1} = \sum_{x=1}^{15} (-1)^{1} x^{14}C_{x-1}$
 $=15 - ({}^{14}C_{0} + {}^{14}C_{1} - \dots -1^{16}C_{1}) = 15(0) = 0$
 $S_{2} = {}^{13} - (-1)^{1} x^{14}C_{x-1}$
 $=15 - ({}^{14}C_{0} + {}^{14}C_{1} + {}^{14}C_{1}) - {}^{16}C_{1} = 2^{13} - 14$
 $S_{1} = S_{1} = 2^{10} - 14$
 $S_{1} = S_{1} = 2^{10} - 14$ <

Final_Jee-Main_24-Feb-2021_Shift-01_Q.Paper (NUMERICAL VALUE TYPE)

This section contains 10 questions. Each question is numerical value type. For each question, enter the correct numerical value (in decimal notation, truncated/rounded-off to second decimal place. (e.g. 6.25, 7.00, 0.33, 30, 30.27, 127.30). Attempt any five questions out of 10. Marking scheme: +4 for correct answer, 0 if not attempted and 0 in all other cases.

81. If one of the diameters of the circle $x^2 + y^2 - 2x - 6y + 6 = 0$ is a chord of another circle

'C', whose centre is at (2, 1), then is radius is _____

Key: 3



Sol:

distance between (1, 3) and (2, 1) is $\sqrt{5}$

$$\therefore \left(\sqrt{5}\right)^2 + \left(2\right)^2 = r^2$$
$$\implies r = 3$$

82. The minimum value of α for which the equation $\frac{4}{\sin x} + \frac{1}{1 - \sin x} = \alpha$ has at least one

solution in
$$\left(0,\frac{\pi}{2}\right)$$
 is _____.

Key: 9

Sol: Let
$$f(x) = \frac{4}{\sin x} + \frac{1}{1 - \sin x}$$

 $y = \frac{4 - 3\sin x}{\sin x(1 - \sin x)}$
Let $\sin x = t$ when $t \in (0,1)$
 $y = \frac{4 - 3t}{t - t^2}$
 $\frac{dy}{dt} = \frac{-3(t - t^2) - (1 - 2t)(4 - 3t)}{(t - t^2)^2} = 0$
 $\Rightarrow 3t^2 - 3t - (4 - 11t + 6t^2) = 0$
 $\Rightarrow 3t^2 - 8t + 4 = 0$

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$$\left(\sin^{-1}\frac{2}{3},9\right)$$

$$\Rightarrow$$
t = $\frac{2}{3}$

$$\Rightarrow \alpha \ge 9$$

Least α is equal to 9

83. Let three vectors \vec{a} , \vec{b} and \vec{c} be such that \vec{c} is coplanar with \vec{a} and \vec{b} , \vec{a} . $\vec{c} = 7$ and \vec{b} is perpendicular to \vec{c} , where $\vec{a} = -\hat{i} + \hat{j} + \hat{k}$ and $\vec{b} - 2\hat{i} + \hat{k}$, then the value of $2|\vec{a} + \vec{b} + \vec{c}|^2$ is

Key: 75

Sol:
$$\vec{c} = \lambda \left(\vec{b} \times (\vec{a} \times \vec{b}) \right)$$

$$= \lambda \left((\vec{b}.\vec{b})\vec{b} - (\vec{b}.\vec{a})\vec{b} \right)$$

$$= \lambda \left(5\left(-\hat{i} + \hat{j} + \hat{k}\right) + 2\hat{i} + \hat{k} \right)$$

$$= \lambda \left(-3\hat{i} + 5\hat{j} + 6\hat{k}\right)$$

$$\vec{c}.\vec{a} = 7 \Longrightarrow 3\lambda + 5\lambda + 6\lambda = 7$$

$$\lambda = \frac{1}{2}$$

$$\therefore 2 \left| \left(\frac{-3}{2} - 1 + 2\right)\hat{i} + \left(\frac{5}{2} + 1\right)\hat{j} + (3 + 1 + 1)\hat{k} \right|^2$$

$$= 2 \left(\frac{1}{4} + \frac{49}{4} + 25\right) = 25 + 50 = 75$$

84. If $\int_{-a}^{a} (|x|+|x-2|) dx - 22$, (a > 2) and [x] denotes the greatest integer $\le x$, then $\int_{a}^{-a} (x + [x]) dx$ is equal to _____.

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Sol:
$$\int_{-a}^{0} (-2x+2)dx + \int_{0}^{2} (x+2+2)dx + \int_{2}^{a} (2x-2)dx = 22$$

$$x^{2} - 2x |_{0}^{-a} + 2x |_{0}^{2} + x^{2} - 2x |_{2}^{a} = 22$$

$$a^{2} + 2a + 4 + a^{2} - 2a - (4-4) = 22$$

$$2a^{2} = 18 \Rightarrow a = 3$$

$$\int_{-3}^{3} (x + [x])dx = -3 - 2 - 1 + 1 + 2 = -3$$
85. Let $P = \begin{bmatrix} 3 & -1 & -2 \\ 2 & 0 & \alpha \\ 3 & -5 & 0 \end{bmatrix}$, where $\alpha \in \mathbb{R}$. Suppose $Q = [q_{if}]$ is a matrix satisfying $PQ = kl_{3}$

for some non-zero $k \in \mathbb{R}$. If $q_{23} = -\frac{k}{8}$ and $|Q| = \frac{k^2}{2}$, then $\alpha^2 + k^2$ is equal to _____.

Key: 17

Sol: As
$$PQ = kI$$
 $\Rightarrow Q = kP^{-1}I$
now $Q = \frac{k}{|P|} (adjP)I \Rightarrow Q = \frac{k}{(20+12\alpha)} \begin{bmatrix} - & - & - \\ - & - & (-3\alpha - 4) \\ - & - & - \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$
 $\therefore q_{23} = -\frac{k}{8} \Rightarrow \frac{k}{(20+12\alpha)} (-3\alpha - 4) = -\frac{k}{8} \Rightarrow 2(3\alpha + 4) = 5 + 3\alpha$
 $3\alpha = -3 \Rightarrow \alpha = -1$
also $|Q| = \frac{k^3 |I|}{|P|} \Rightarrow \frac{k^2}{2} = \frac{k^3}{(20+12\alpha)}$
 $(20+12\alpha) = 2k \Rightarrow 8 = 2k \Rightarrow k = 4$

86. Let $B_f(i=1,2,3)$ be three independent events in a sample space. The probability that only B_1 occur is α , only B_2 occurs is β and only B_3 occurs is γ . Let p be the probability that none of the events B_f occurs and these 4 probabilities satisfy the equations $(\alpha - 2\beta)p = \alpha\beta$ and $(\beta - 3\gamma)p = -2\beta\gamma$ (All the probabilities are assumed to lie in the interval (0, 1). Then $\frac{P(B_1)}{P(B_3)}$ is equal to ______.

Key: 6

Sol: Let x, y, z be probability of B_1 , B_2 , B_3 respectively

$$\Rightarrow x(1-y)(1-z) = \alpha \Rightarrow y(1-x)(1-z) = \beta$$
$$\Rightarrow z(1-x)(1-y) = \gamma \Rightarrow (1-x)(1-z) = P$$

Putting in the given relation we get x = 2y and $y = 3z \implies x = 6z \implies \frac{x}{z} = 6$

87. Let $A = \{n \in N : n \text{ is } a 3 - digit number} B - \{9k + 2; k \in N\}$ and $C - \{9k + 1; k \in N\}$ for some $l \ (0 < l < 9)$

If the sum of all elements of the set $A \cap (B \cap C)$ is 274×400 , then *l* is equal to _____

Key: 5

Sol: 3 digit number of the form 9K + 2 are {101,109,....,992}

$$\Rightarrow$$
 Sum equal to $\frac{100}{2}(1093)$

Similarly sum of 3 digit number of the form 9K + 5 is $\frac{100}{2}(1099)$

$$\frac{100}{2}(1093) + \frac{100}{2}(1099) = 100 \times (1096)$$
$$= 400 \times 274 \longrightarrow l = 5$$

88. If the least and the largest real values of α , for which the equation $z + \alpha |z - 1| + 2i = 0 (z \in C \text{ and } i = \sqrt{-1})$ has a solution, are p and q respectively, then $4(p^2 + q^2)$ is equal to_____.

Sol:
$$x + iy + \alpha \sqrt{(x-1)^2 + y^2} + 2i = 0$$

 $\therefore y + 2 = 0 \& x + \alpha \sqrt{(x-1)^2 + y^2} = 0$
 $y = -2 \& x^2 = \alpha^2 (x - 2x + 1 + 4)$
 $\alpha^2 = \frac{x^2}{x^2 - 2x + 5}$
 $\therefore \alpha^2 \in \left[0, \frac{5}{4}\right]$

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$$\therefore \alpha^2 \in \left[-\frac{\sqrt{5}}{2}, \frac{\sqrt{5}}{2}\right]$$

Then $4\left[\left(\alpha_{\max}\right)^2 + \left(\alpha_{\min}\right)^2\right] = 4\left[\frac{5}{4} + \frac{5}{4}\right] = 10$

89. Let M be any 3×3 matrix with entries from the set $\{0, 1, 2\}$. Then maximum number of such matrices, for which the sum of diagonal elements of M^TM is seven, is _____

Sol:
$$\begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} a & d & g \\ b & e & h \\ c & f & i \end{bmatrix}$$
$$a^{2} + b^{2} + c^{2} + d^{2} + e^{2} + f^{2} + g^{2} + h^{2} + i^{2} = 7$$
Case I : Seven (1's) and two (0's)
$${}^{9}C_{2} = 36$$
Case- II : One (2) and three (1's) and five (0's)
$$\frac{9!}{5!3!} = 504$$
$$\therefore Total = 540$$
90.
$$\lim_{n \to \infty} \tan \left\{ \sum_{r=1}^{n} \tan^{-1} \left(\frac{1}{1+r+r^{2}} \right) \right\} \text{ is equal to } \underline{\qquad}$$
Key: 1
Sol:
$$\tan \left(\lim_{n \to \infty} \sum_{r=1}^{n} \left[\tan^{-1} (r+1) - \tan^{-1} (r) \right] \right)$$
$$= \tan \left(\lim_{n \to \infty} \left(\tan^{-1} (n+1) - \frac{\pi}{4} \right) \right)$$
$$= \tan \left(\frac{\pi}{4} \right) = 1$$