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# JEE MAIN 2026 - SESSION 1

24-01-2026 - Shift 1

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## 24-Jan-2026\_Shift-I\_JEE Main-2026\_Session-I(Jan)

### MATHEMATICS

Max Marks: 100

#### SECTION-I

#### (SINGLE CORRECT ANSWER TYPE)

This section contains **20 Multiple Choice Questions**. Each question has 4 options (1), (2), (3) and (4) for its answer, out of which **ONLY ONE** option can be correct.

**Marking scheme: +4 for correct answer, 0 if not attempted and -1 in all other cases.**

1. Let  $S = \left\{ Z \in \mathbb{C} : \left| \frac{Z-6i}{Z-2i} \right| = 1 \text{ and } \left| \frac{z-8+2i}{z+2i} \right| = \frac{3}{5} \right\}$  then  $\sum_{Z \in S} |Z|^2$  is equal to

- 1) 385                      2) 413                      3) 398                      4) 423

**Key: 1**

**Sol:**  $\left| \frac{Z-6i}{Z-2i} \right| = 1 \Rightarrow y = 4$

$$25|z-8+2i|^2 = 9|z+2i|^2$$

$$\Rightarrow x^2 + y^2 - 25x + 4y + 104 = 0$$

Points are (17,4), (8,4)

2. If the function  $f(x) = \frac{e^x (e^{\tan x - x} - 1) + \log_e (\sec x + \tan x) - x}{\tan x - x}$  is continuous at

$x=0$  then the value of  $f(0)$  is equal to

- 1)  $\frac{3}{2}$                       2) 2                      3)  $\frac{1}{2}$                       4)  $\frac{2}{3}$

**Key: 1**

**Sol:**  $f(0) = \lim_{x \rightarrow 0} e^x \frac{(e^{\tan x - x} - 1)}{\tan x - x} + \lim_{x \rightarrow 0} \frac{\log(\sec x + \tan x) - x}{\tan x - x}$

$$\lim_{x \rightarrow 0} e^x \frac{[e^{\tan x - x} - 1]}{\tan x - x} - 1 \lim_{x \rightarrow 0} \frac{\log(\sec x + \tan x) - x}{\tan x - x}$$

$$e^{(0)}(1) + \lim_{x \rightarrow 0} \frac{\frac{1}{\sec x + \tan x} \cdot (\sec x \tan x + \sec^2 x) - 1}{\sec^2 x - 1} \text{ L'Hospital rule}$$

$$= 1 + \lim_{x \rightarrow 0} \frac{\sec x - 1}{(\sec x - 1)(\sec x + 1)} = 1 + \frac{1}{2} = \frac{3}{2}$$

3. Let a circle of radius 4 pass through the origin O. The Points  $A(-\sqrt{3}a, 0)$  and  $B(0, -\sqrt{2}b)$  where a and b are real parameters  $ab \neq 0$ . Then the locus of the centroid  $\Delta OAB$  is circle of radius

1)  $\frac{7}{3}$                       2)  $\frac{11}{3}$                       3)  $\frac{8}{3}$                       4)  $\frac{5}{3}$

**Key:** 3

**Sol:**  $R = 4 \Rightarrow R^2 = 16 \Rightarrow 2b^2 + 3a^2 = 64$

$$b = \frac{-3x}{\sqrt{2}}, a = \frac{-3y}{\sqrt{3}}$$

$$2b^2 + 3a^2 = 64$$

$$\Rightarrow x^2 + y^2 = \left(\frac{8}{3}\right)^2$$

$$\therefore r = \frac{8}{3}$$

4. Consider an A.P :  $a_1, a_2, a_3, \dots, a_n; a_1 > 0$  If  $a_2 - a_1 = \frac{-3}{4}, a_n = \frac{1}{4}a_1$  and  $\sum_{i=1}^n a_i = \frac{525}{2}$  then  $\sum_{i=1}^{17} a_i$  is equal to

1) 476                      2) 136                      3) 952                      4) 238

**Key:** 4

**Sol:**  $a_2 - a_1 = -\frac{3}{4} \Rightarrow a_1 + d - a_1 = -\frac{3}{4} \Rightarrow d = -\frac{3}{4}$

$$a_n = \frac{1}{4}a_1 \Rightarrow a_1 + (n-1) \cdot \left(-\frac{3}{4}\right) = \frac{1}{4}a_1$$

$$\Rightarrow 4a_1 - 3n + 3 = a_1 \Rightarrow 3a_1 - 3n + 3 = 0 \Rightarrow a_1 - n + 1 = 0$$

$$\sum_{i=1}^n a_i = \frac{525}{2} \Rightarrow \frac{n}{2} \left[ 2a_1 + (n-1) \cdot \left(-\frac{3}{4}\right) \right] = \frac{525}{2} \Rightarrow \frac{n}{2} [a_1 + a_n] = \frac{525}{2}$$

$$8na_1 - 3n^2 + 3n = 525 \Rightarrow \frac{n}{2} \left[ a_1 + \frac{a_1}{4} \right] = \frac{525}{2}$$

$$\Rightarrow a_n n = 420$$

$$\Rightarrow a_1 [a_1 + 1] = 420 = 20 \times 21$$

$$\Rightarrow a_1 = 20$$

$$\sum_{i=1}^{17} ai = \frac{17}{2} [a_1 + a_n] = \frac{17}{2} \left[ 40 + 16 \left(-\frac{3}{4}\right) \right] = 238$$

$$= \frac{17}{2} \left[ \frac{5a_1}{4} \right] = \frac{17}{2} \times \frac{5}{4} \times 20$$

5. Let  $\alpha, \beta \in \mathbb{R}$  such that the function  $f(x) = \begin{cases} 2\alpha(x^2 - 2) + 2\beta x, & x < 1 \\ (\alpha + 3)x + \alpha - \beta, & x \geq 1 \end{cases}$  be differentiable at all  $x \in \mathbb{R}$

then  $34(\alpha + \beta) =$

- 1) 24                      2) 84                      3) 48                      4) 36

**Key: 3**

**Sol:**  $f(x) = \begin{cases} 2x(x^2 - 2) + 2\beta x, & x < 1 \\ (\alpha + 3)x + \alpha - \beta, & x \geq 1 \end{cases}$

$$f(1^-) = f(1^+) = 2\alpha(-1) + 2\beta(1) = (\alpha + 3) + \alpha - \beta \Rightarrow 4\alpha - 3\beta + 3 = 0 \rightarrow (1)$$

$$f'(x) = \begin{cases} 2\alpha(2x) + 2\beta & x < 1 \\ (\alpha + 3) & x \geq 1 \end{cases}$$

$$f'(1^-) = f'(1^+) \Rightarrow 4\alpha + 2\beta = \alpha + 3 \Rightarrow 3\alpha + 2\beta - 3 = 0 \rightarrow (2)$$

Solving (1), (2) we get  $\alpha = 3m$   $\beta = \frac{21}{17}$

$$\therefore 34(\alpha + \beta) = 48$$

$$-2\alpha + 2\beta\alpha = 2\alpha$$

$$4\alpha - 2\alpha\beta = 0 \Rightarrow 2\alpha(2 - \beta) = 0$$

$$\beta = 2$$

$$4\alpha = \alpha + \beta$$

$$3\alpha = \beta \Rightarrow \alpha = \frac{2}{3}$$

$$34 \left[ \frac{2}{3} + 2 \right]$$

$$34 \left[ \frac{2+6}{3} \right]$$

6. Let  $f(t) = \int \left( \frac{1 - \sin(\log_e t)}{1 - \cos(\log_e t)} \right) dt, t > 1$ . if  $f(e^{\pi/2}) = -e^{\pi/2}$  and  $f(e^{\pi/4}) = \alpha e^{\pi/4}$  then  $\alpha$  equals

- 1)  $-1 - 2\sqrt{2}$               2)  $-1 + \sqrt{2}$               3)  $-1 - \sqrt{2}$               4)  $1 + \sqrt{2}$

**Key: 3**

**Sol:** Let  $\cos t = x \Rightarrow t = e^x \Rightarrow dt = e^x dx$

$$G.I = \int \frac{1 - \sin x}{2 \sin^2 \frac{x}{2}} e^x dx = \frac{1}{2} \int \left( \operatorname{cosec}^2 \frac{x}{2} - 2 \cot \frac{x}{2} \right) e^x dx = \frac{1}{2} e^x \left( -2 \cot \frac{x}{2} \right) + c \Rightarrow -t \cot \left( \frac{\log t}{2} \right) + c$$

$$f(e^{-\pi/2}) = -e^{\pi/2} \Rightarrow c = 0$$

$$\therefore d(e^{\pi/4}) = -e^{-\pi/4} (\sqrt{2} + 1)$$

$$\therefore \alpha = -(\sqrt{2} + 1)$$

7. Let  $S = \frac{1}{25!} + \frac{1}{3!23!} + \frac{1}{5!21!} + \dots$  Up to 13 terms. If  $13S = \frac{2^k}{n!}$ ,  $k \in \mathbb{N}$  then  $n + k$  is equal to

- 1) 49                      2) 51                      3) 52                      4) 50

**Key: 1**

$$\text{Sol: } S = \frac{1}{26!} \left[ \frac{26!}{25!1!} + \frac{26!}{5!21!} + \dots + 13 \text{ terms} \right] = \frac{1}{26!} \left[ {}^{26}C_1 + {}^{26}C_3 + \dots + {}^{26}C_{25} \right] = \frac{2^{25}}{26!}$$

$$\therefore 13S = \frac{2^{25}}{26!} \times 13 = \frac{2^{25}}{2 \times 13 \times 25!} \times 13 = \frac{2^{24}}{25!} \therefore n + k = 49$$

8. The number of real solutions of a the equation  $x|x+3| + |x-1| - 2 = 0$  is

- 1) 3                      2) 5                      3) 2                      4) 4

**Key: 1**

$$\text{Sol: } x|x+3| + |x-1| - 2 = 0$$

$$x \leq -3 \Rightarrow x(x+3) + 1 - x - 2 = 0 \Rightarrow x^2 + 4x + 1 = 0$$

$$x = \frac{-4 \pm \sqrt{16-4}}{2} \quad -3 < x \leq 1 \Rightarrow x^2 + 3x + 1 - x - 2 = 0$$

$$x^2 + 2x - 1 = 0 \quad x = \frac{-2 + \sqrt{4+4}}{2}$$

$$x > 1 \quad x^2 + 3x + x - 1 - 2 = 0$$

$$x^2 + 4x - 3 = 0 \quad x = \frac{-4 \pm \sqrt{16+12}}{2} = \frac{-4 \pm 2\sqrt{7}}{2}$$

9. Let the lines  $L_1: \vec{r} = \hat{i} + 2\hat{j} + 3\hat{k} + \lambda(2\hat{i} + 3\hat{j} + 4\hat{k})$ ,  $\lambda \in \mathbb{R}$ , and  $L_2: \vec{r} = (4\hat{i} + \hat{j}) + \mu(5\hat{i} + 2\hat{j} + \hat{k})$ ,  $\mu \in \mathbb{R}$

intersect at the point R. Let P and Q be the points lying on the lines  $L_1$  and  $L_2$

respectively such that  $|PR| = \sqrt{29}$  and  $|PQ| = \sqrt{\frac{47}{3}}$  and  $|PQ| = \sqrt{\frac{47}{3}}$  if the Point P lies in the 1<sup>st</sup>

octant then  $27(QR)^2$  is equal to

- 1) 340                      2) 348                      3) 360                      4) 320

**Key: 3****Sol:** Finding point  $R(-1, -1, -1)$ 

$$P(2\lambda + 1, 3\lambda + 2, 4\lambda + 3)Q(5\mu + 4, 2\mu + 1, \mu)$$

$$|PQ| = \sqrt{\frac{47}{3}} \Rightarrow (5\mu + 3)^2 + (2\mu - 1)^2 + (\mu - 3)^2 = \frac{47}{3} \Rightarrow \mu = \frac{1}{3}$$

$$PQ = \sqrt{29} \Rightarrow (2\lambda + 2)^2 + (3\lambda + 3)^2 + (4\lambda + 4)^2 = 29$$

$$\therefore Q = \left(\frac{7}{3}, \frac{1}{3}, -\frac{1}{3}\right)$$

$$\therefore (QR)^2 = \frac{120}{9} \Rightarrow 27(QR)^2 = 27 \times \frac{120}{9} = 360$$

10. From a lot containing 10 defective and 90 and defective bulbs, 8 bulbs are selected one by one with replacement then the probability of getting at least 7 defective bulbs is

- 1)  $\frac{7}{10^7}$                       2)  $\frac{81}{10^8}$                       3)  $\frac{73}{10^8}$                       4)  $\frac{67}{10^8}$

**Key: 3****Sol:** required probability

$$= P(X = 7) + P(X = 8) = P(7 \text{ defective, } 1 \text{ fair}) + P(8 \text{ defective})$$

$$= \frac{10^7 \times 90 \times 8 + 10^8}{100^8} = \frac{10^8 [72 + 1]}{(100)^8}$$

11. Let  $A(1,0)$   $B(2,-1)$  and  $C = \left(\frac{7}{3}, \frac{4}{3}\right)$  be three points. If the equation of bisector of the angle ABC is  $\alpha x + \beta y = 5$  then the value of  $\alpha^2 + \beta^2$  is

- 1) 8                      2) 5                      3) 10                      4) 13

**Key: 3**

$$\text{Sol: } AD : DC = BA : BC = \sqrt{1+1} : \sqrt{\frac{1}{9} + \frac{49}{9}} = 3:5$$

$$D = \frac{3\left(\frac{7}{3}, \frac{4}{3}\right) + 5(1,0)}{3+5} = \left(\frac{12}{8}, \frac{4}{8}\right) = \left(\frac{3}{2}, \frac{1}{2}\right)$$

$$\text{Equation of BD is } 3x + y - 5 = 0 \quad \alpha^2 + \beta^2 = 10$$

12. The value of  $\frac{\sqrt{3} \operatorname{cosec} 20^\circ - \sec 20^\circ}{\cos 20^\circ \cos 40^\circ \cos 60^\circ \cos 80^\circ}$  is equal to

- 1) 16                      2) 12                      3) 64                      4) 32

**Key: 3**

**Sol:** 
$$\frac{2\left(\frac{\sqrt{3}}{2}\cos 20^\circ - \frac{1}{2}\sec 20^\circ\right)}{\frac{1}{2} \times \frac{1}{4} \times \frac{1}{2}} = 64$$

13. If the Domain of the function  $f(x) = \log_{(10x^2 - 17x + 7)}(18x^2 - 11x + 1)$  is  $(-\infty, a) \cup (b, c) \cup (d, \infty) - \{e\}$  then  $90(a + b + c + d + e)$  equals
- 1) 307                      2) 177                      3) 316                      4) 170

**Key:** 3

**Sol:**  $|8x^2 - 11x + 1| > 0$   $|10x^2 - 17x + 7| > 0, \neq 1$

$$x \in \left(-\infty, \frac{1}{9}\right) \cup \left(\frac{1}{2}, \infty\right) \quad x \in \left(-\infty, \frac{7}{10}\right) \cup (1, \infty) \quad x \neq \frac{6}{5}, \frac{1}{2}$$

$$\therefore x \in \left(-\infty, \frac{1}{9}\right) \cup \left(\frac{1}{2}, \frac{7}{10}\right) \cup (1, \infty) - \left\{\frac{6}{5}\right\} \quad a + b + c + d + e = 3/6$$

14. The mean and variance of data of 10 observations are 10 and 2 respectively. If an observation  $\alpha$  in this data is replaced by  $\beta$ , then the mean and variance become 10.1 and 1.99 respectively then  $\alpha + \beta$  equals
- 1) 10                      2) 15                      3) 20                      4) 5

**Key:** 3

**Sol:** Let be data  $x_1, x_2, \dots, x_a, \alpha$

$$\sum_{i=1}^9 x_i = 100 - \alpha$$

$$\sum x_i^2 = 1020 - \alpha^2$$

$$100 - \alpha + \beta = 101 \quad \alpha - \beta + 1$$

$$\frac{\sum_{i=1}^9 x_i^2 + \beta^2}{10} - (101)^2 = 1.99$$

$$\beta^2 \cdot \alpha^2 = 20 \Rightarrow \alpha = \frac{19}{2}, \beta = \frac{21}{2}$$

$$\alpha + \beta = 20$$

15. If  $\cot x = \frac{5}{12}$  for some  $x \in \left(\pi, \frac{3\pi}{2}\right)$  then  $\sin 7x \left(\cos \frac{13x}{2} + \sin \frac{13x}{2}\right) + \cos 7x \left(\cos \frac{13x}{2} - \sin \frac{13x}{2}\right)$  is equal to
- 1)  $\frac{1}{\sqrt{13}}$                       2)  $\frac{4}{\sqrt{26}}$                       3)  $\frac{5}{\sqrt{13}}$                       4)  $\frac{6}{\sqrt{26}}$

**Key: 1**

**Sol:**  $\sin 7x \left( \cos \frac{13x}{2} + \frac{13x}{2} \right) + \cos \left( \cos \frac{13x}{2} - \sin \frac{13x}{2} \right)$

$$\sin \left( 7x - \frac{13x}{2} \right) + \cos \left( 7x - \frac{13x}{2} \right) = \sin \frac{x}{2} + \cos \frac{x}{2} = \pm \sqrt{\frac{1 - \cos x}{2}} \pm \sqrt{\frac{1 + \cos x}{2}}$$

$$= \pm \sqrt{\frac{1 + \frac{5}{13}}{2}} \pm \sqrt{\frac{1 - \frac{5}{13}}{2}} = \sqrt{\frac{18}{2 \times 13}} - \sqrt{\frac{8}{2 \times 13}} = \frac{3}{\sqrt{13}} - \frac{1}{\sqrt{13}} = \frac{1}{\sqrt{13}}$$

$$x \in \left( \pi, \frac{3\pi}{2} \right)$$

$$\frac{x}{2} \in \left( \frac{\pi}{2}, \frac{3\pi}{4} \right)$$

16. Let each of the two ellipses  $E_1 : \frac{x^2}{a^2} + \frac{y^2}{b^2} = 1 (a > b)$  and  $E_2 : \frac{x^2}{A^2} + \frac{y^2}{B^2} = 1 (A < B)$  have eccentricity  $\frac{4}{5}$ . Let the Length of the latusrecta of  $E_1$  and  $E_2$  be  $l_1, l_2$  respectively such that  $2l_1^2 = 9l_2^2$ .

If the distance between foci of  $E_1$  is 8. Then the difference between foci of  $E_2$  is

- 1)  $\frac{8}{5}$                       2)  $\frac{16}{5}$                       3)  $\frac{32}{5}$                       4) 18

**Key: 3**

**Sol:**  $2ae = 8, e = \frac{4}{5} \Rightarrow \boxed{a = 5}$

$$b^2 = a^2 - a^2 e^2 = 9$$

$$2l_1^2 = 9l_2^2 \Rightarrow 2 \left( \frac{18}{5} \right)^2 = 9 \frac{2A^2}{B}$$

$$A^2 = B^2 (1 - e^2)$$

$$\Rightarrow B = 4$$

$$\therefore \text{Required} = 2Be = 2 \cdot 4 \cdot \frac{4}{5} = \frac{32}{5}$$

17. Let R be relation defined on the set  $\{1, 2, 3, 4\} \times \{1, 2, 3, 4\}$  by

$R = \{((a, b)(c, d)) : 2a + 3b = 3c + 4d\}$  then the number of elements in R is

- 1) 6                              2) 15                              3) 12                              4) 13

**Key: 3**

**Sol:**  $(a, b) \rightarrow (c, d)$

(1,1) → No values

(1,2) → No values

(1,3) → (1,2)

(1,4) → (2,2)

(2,1) → (1,1)

(2,2) → (2,1)

(2,3) → (3,1)

(2,4) → (4,1)

(3,1) → No values

(3,2) → No values

(3,3) → (1,3)

(3,4) → (2,3)

(4,1) → (1,2)

(4,2) → (2,2)

(4,3) → (3,2)

(4,4) → (2,2)

Number of elements = 12

18. Let 729, 81, 9, 1.....be a sequence and  $P_n$  denote the product of the first  $n$  terms of thesequence. If  $2 \sum_{n=1}^{40} (P_n)^{\frac{1}{n}} = \frac{3^\alpha - 1}{3^\beta}$  and gcd of  $(\alpha, \beta) = 1$  then  $\alpha + \beta$  is equal to

1) 79

2) 73

3) 76

4) 75

**Key:** 2**Sol:**  $P_n = 3^{6+4+2+\dots+1} = 3^{n(n+1)} \Rightarrow P_n^{1/n} = 3^{n+1}$ 

$$\sum_{n=1}^{40} (P_n)^{1/n} = 3^6 + 3^5 + \dots + 3^1 = 3^6 \left[ \frac{1 - \left(\frac{1}{3}\right)^{40}}{1 - \frac{1}{3}} \right] = \frac{3^{40} - 1}{2 \cdot 3^{33}}$$

 $\therefore \alpha = 40, \beta = 33$

19. Let  $A_1$  the bounded area enclosed by the curves  $y = x^2 + 2$ ,  $x + y = 8$  and  $y$ -axis that lies in the first quadrant. Let  $A_2$  be bounded area enclosed by the curves  $y = x^2 + 2$ ,  $y^2 = x$ ,  $x = 2$  and  $y$ -axis that lies in the first quadrant then  $A_1 - A_2$  is equal to

- 1)  $\frac{2}{3}(2\sqrt{2} + 1)$       2)  $\frac{2}{3}(\sqrt{2} + 1)$       3)  $\frac{2}{3}(3\sqrt{2} + 1)$       4)  $\frac{2}{3}(4\sqrt{2} + 1)$

**Key: 1**

**Sol:**

$$y = x^2 + 2$$

$$8 - x = x^2 + 2$$

$$\Rightarrow x^2 + x - 6 = 0 \quad \Rightarrow (x - 2)(x + 3) = 0 \quad \Rightarrow x = 2, x = -3$$

$$A_1 = \int_0^2 [(8 - x)(x^2 + 2)] dx$$

$$= \int_0^2 (6 - x - x^2) dx = \left[ 6x - \frac{x^2}{2} - \frac{x^3}{3} \right]_0^2 = \left[ \left( 12 - 2 - \frac{8}{3} \right) - 0 \right] = \frac{22}{3}$$

$$A_2 = \int_0^2 (x^2 + 2 - \sqrt{x}) dx = \left[ \frac{x^3}{3} + 2x - \frac{2}{3}x^{3/2} \right]_0^2 = \left[ \left( \frac{8}{3} + 4 - \frac{2}{3} \cdot 2\sqrt{2} \right) - 0 \right] = \frac{20}{3} - \frac{2}{3} \cdot 2\sqrt{2}$$

20. Let  $\vec{a} = 2\hat{i} + \hat{j} - 2\hat{k}$ ,  $\vec{b} = \hat{i} + \hat{j}$  and  $\vec{c} = \vec{a} \times \vec{b}$ . Let  $\vec{d}$  be a vector such that  $|\vec{d} - \vec{a}| = \sqrt{11}$ ,  $|\vec{c} \times \vec{d}| = 3$  and angle between  $\vec{c}$  and  $\vec{d}$  is  $\frac{\pi}{4}$ . Then  $\vec{a} \cdot \vec{d}$  is equal to

- 1) 11      2) 0      3) 1      4) 3

**Key: 2**

**Sol:**  $\vec{c} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 2 & 1 & -2 \\ 1 & 1 & 0 \end{vmatrix} = \hat{i}(2) - \hat{j}(2) + \hat{k}(1)$

$$|\vec{c} \times \vec{d}| = 3 \Rightarrow |\vec{c}| |\vec{d}| \sin(\vec{c}, \vec{d}) = 3 \Rightarrow 3 |\vec{d}| \frac{1}{\sqrt{2}} = 3$$

$$|\vec{d}| = \sqrt{2}$$

$$|\vec{d} - \vec{a}| = \sqrt{11} \Rightarrow \vec{d}^2 + \vec{a}^2 - 2\vec{a} \cdot \vec{d} = 11 \Rightarrow \vec{d}^2 + 9 - 2\vec{a} \cdot \vec{d} = 11 \Rightarrow \vec{a} \cdot \vec{d} = 0$$

**SECTION-II**  
**(NUMERICAL VALUE TYPE)**

This section contains **5 Numerical Value Type Questions**. The Answer should be within **0 to 9999**. If the Answer is in **Decimal** then round off to the **Nearest Integer** value (Example i.e. If answer is above **10** and less than **10.5** round off is **10** and if answer is from **10.5** and less than **11** round off is **11**).

**Marking scheme: +4 for correct answer, 0 if not attempted and -1 in all other cases.**

21. The number of numbers greater than 5000, less than 9000 and divisible by 3, that can be formed using the digits 0, 1, 2, 5, 9, if the repetition of the digits is allowed is \_\_\_\_

**Key: 42**

**Sol:** conceptual

22. Let a differentiable function  $f$  satisfy the equation  $\int_0^{36} f\left(\frac{tx}{36}\right) dt = 4\alpha f(x)$ .

If  $y = f(x)$  is a standard parabola passing through the points  $(2,1)$  and  $(-4,\beta)$  then  $\beta^\alpha$  is equal to \_\_\_\_\_

**Key:** 64

**Sol:**  $\int_0^{36} f\left(\frac{tx}{36}\right) dt \cdot \frac{tx}{36} = y dt = \frac{36}{x} dy$

$$\therefore \int_0^x \frac{f(y)36 dy}{x} = 4\alpha + f(x)$$

$$\int_0^x f(y) dy = \frac{\alpha \cdot x \cdot f(x)}{9} \Rightarrow f(x) = \frac{\alpha}{9} (f + xf')$$

$$\frac{f'(x)}{f(x)} = \left(\frac{9}{\alpha} - 1\right) \frac{1}{x} \Rightarrow f(x) = c x^{\left(\frac{9}{\alpha} - 1\right)} (2,1)$$

$$\alpha = 3, c = \frac{1}{4} \left[ \because \frac{9}{\alpha} - 1 = 2 \right]$$

$$y = \frac{x^2}{4} \hat{=} (-4, \beta) \text{ parabola} \Rightarrow \beta = 4$$

$$\beta^\alpha = 64$$

23. The number of  $3 \times 2$  matrices  $A$ , which can be formed using the elements of the set  $\{-2, -1, 0, 1, 2\}$  such that the sum of all the diagonal elements of  $A^T A$  is 5, is \_\_\_\_\_

**Key:** 312

**Sol:**  $A = \begin{bmatrix} a & b \\ c & d \\ e & f \end{bmatrix}$  sum of diagonal elements of  $A^T A$  is 5  $\Rightarrow a^2 + b^2 + c^2 + d^2 + e^2 + f^2 = 5$

by verification the number of matrices is 312.

24. Let  $(2\alpha, \alpha)$  be the largest interval in which the function  $f(t) = \frac{|t+1|}{t^2}$ ,  $t < 0$  is strictly decreasing. Then the local maximum value of the function

$$g(x) = 2 \log_e (x-2) + ax^2 + 4x - \alpha, x > 2, \text{ is } \underline{\hspace{2cm}}$$

**Key:** 4

**Sol:**  $\left(\frac{t+1}{t^2}\right)$  is decreasing in  $(-2, -1)$

$$\alpha = -1$$

$$g(x) = \log(x-2) - x^2 + 4x + 1$$

$$g'(x) = -\frac{(x-3)(x-1)}{x-2}$$

$$g(x) \text{ has maximum at } x=3 \Rightarrow g(3) = 4$$

25. Let a line L passing through the point P (1,1,1) be perpendicular to the lines

$$\frac{x-4}{4} = \frac{y-1}{1} = \frac{z-1}{1} \text{ and } \frac{x-17}{1} = \frac{y-71}{1} = \frac{z}{0}. \text{ Let the line L intersect the } yz\text{-plane at the point}$$

Q. Another line parallel to L and passing through the point S(1,0,-1) intersects the yz-plane at point R. Then the square of the area of the parallelogram PQRS is equal to \_\_\_\_\_

**Key:** 6

**Sol:**  $\vec{a} \times \vec{b} = -\hat{i} + \hat{j} + 3\hat{k}$

$$1: \frac{x-1}{-1} = \frac{y-1}{1} = \frac{z-1}{3} = \lambda$$

$$(0, 2, 4), \text{ Area} = |\overline{PQ} \times \overline{PS}| = \sqrt{6}$$

## PHYSICS

Max Marks: 100

SECTION-I  
(SINGLE CORRECT ANSWER TYPE)

This section contains **20 Multiple Choice Questions**. Each question has 4 options (1), (2), (3) and (4) for its answer, out of which **ONLY ONE** option can be correct.

**Marking scheme: +4 for correct answer, 0 if not attempted and -1 in all other cases.**

26. Density of water  $4^\circ\text{C}$  and  $20^\circ\text{C}$  are  $1000\text{kg/m}^3$  and  $998\text{kg/m}^3$  respectively the increase in internal energy of  $4\text{kg}$  of water when it is heated from  $4^\circ\text{C}$  to  $20^\circ\text{C}$  is \_\_\_\_ J.

(specific heat capacity of water =  $4.2\text{J/kg}$  and 1 atmospheric pressure =  $10^5\text{Pa}$ )

- 1) 268799.2      2) 315826.2      3) 258700.8      4) 234699.2

**Key: 1**

**Sol:**  $Q = msdt = 4 \times 4200 \times 16 = 268800$

$$W = pdv = p[v_2 - v_1]$$

$$= p \left[ \frac{m}{\rho_2} - \frac{m}{\rho_1} \right]$$

$$= 10^5 \left[ \frac{4}{998} - \frac{4}{1000} \right]$$

$$= \frac{10^5 \times 4 \times 2}{998 \times 1000}$$

$$= 0.8016$$

$$\Delta u = dQ - dw$$

$$= 268800 - 0.8016$$

$$268799.19\text{J}$$

27. In a microscope of tube length  $10\text{cm}$ , two convex lens's are arranged with focal length of  $2\text{cm}$  and  $5\text{cm}$  Total magnification obtained with this system for normal advistament is

(5)<sup>k</sup> the value of K is

- 1) 4      2) 5      3) 2      4) 3.5

**Key: 3**

**Sol:**  $f_o = 2\text{cm}$ ,  $f_e = 5\text{cm}$ ,  $L = 10\text{cm}$

$$\text{Magnification } m = m_o m_e = \frac{L}{f_o} \left( \frac{D}{f_e} \right)$$

$$\therefore m = \frac{10}{2} \left( \frac{25}{5} \right) = 5 (5)$$

$$\therefore \boxed{K = 2}$$

28. Two electrons are moving in orbits of two hydrogen like atoms with speed  $3 \times 10^5 \text{ m/s}$  and  $2.5 \times 10^5 \text{ m/s}$  respectively. If the radii of these orbits are nearly same then, the possible order of energy states are \_\_\_ respectively

- 1) 9 and 8                      2) 10 and 12                      3) 8 and 10                      4) 6 and 5

**Key:** 4

**Sol:**  $E \propto \frac{z^2}{n^2}$  &  $V \propto \frac{z}{n}$

For hydrogen like atom  $E \propto \frac{1}{n^2}$  &  $V \propto \frac{1}{n}$

$$\Rightarrow E \propto V^2 \Rightarrow \frac{E_1}{E_2} = \left( \frac{V_1}{V_2} \right)^2 = \left( \frac{3 \times 10^5}{2.5 \times 10^5} \right)^2 \Rightarrow \frac{E_1}{E_2} = \left( \frac{6}{5} \right)^2 = \frac{36}{25}$$

But  $\frac{E_1}{E_2} = \left( \frac{n_2}{n_1} \right)^2 = \left( \frac{6}{5} \right)^2$

$\therefore$  Possible states are 6 & 5

29. There are three co-centric conducting spherical shell A, B and C radii a, b and c respectively ( $c < b < a$ ) and they are charged with charge  $q_1, q_2$  and  $q_3$  respectively.

The potentials of the spheres A, B and C respectively, are:

1)  $\frac{1}{4\pi\epsilon_0} \left[ \frac{q_1 + q_2 + q_3}{a} \right], \frac{1}{4\pi\epsilon_0} \left[ \frac{q_1 + q_2 + q_3}{b} + \frac{q_3}{c} \right], \frac{1}{4\pi\epsilon_0} \left[ \frac{q_1}{a} + \frac{q_2}{b} + \frac{q_3}{c} \right]$

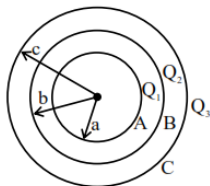
2)  $\frac{1}{4\pi\epsilon_0} \left[ \frac{q_1}{a} + \frac{q_2}{b} + \frac{q_3}{c} \right], \frac{1}{4\pi\epsilon_0} \left[ \frac{q_1 + q_2 + q_3}{b} \right], \frac{1}{4\pi\epsilon_0} \left[ \frac{q_1 + q_2 + q_3}{c} \right]$

3)  $\frac{1}{4\pi\epsilon_0} \left[ \frac{q_1 + q_2 + q_3}{a} \right], \frac{1}{4\pi\epsilon_0} \left[ \frac{q_1 + q_2 + q_3}{b} \right], \frac{1}{4\pi\epsilon_0} \left[ \frac{q_1 + q_2 + q_3}{c} \right]$

4)  $\frac{1}{4\pi\epsilon_0} \left[ \frac{q_1}{a} + \frac{q_2}{b} + \frac{q_3}{c} \right], \frac{1}{4\pi\epsilon_0} \left[ \frac{q_1 + q_2 + q_3}{b} + \frac{q_3}{c} \right], \frac{1}{4\pi\epsilon_0} \left[ \frac{q_1 + q_2 + q_3}{c} \right]$

**Key:** 4

**Sol:**



$$V_A = \frac{1}{4\pi\epsilon_0} \left[ \frac{q_1}{a} + \frac{q_2}{b} + \frac{q_3}{c} \right]$$

$$V_B = \frac{1}{4\pi\epsilon_0} \left[ \frac{q_1 + q_2 + q_3}{b} \right]$$

$$V_C = \frac{1}{4\pi\epsilon_0} \left[ \frac{q_1 + q_2 + q_3}{c} \right]$$

30. An unpolarised light is incident at an interface of two dielectric media having refractive indices of 2 and  $2\sqrt{3}$  respectively to satisfy the condition that reflected and refracted rays are perpendicular to each other, the angle of incidence is \_\_\_\_\_

- 1)  $30^\circ$                       2)  $60^\circ$                       3)  $45^\circ$                       4)  $10^\circ$

**Key:** 2

**Sol:** From Brewster law

$$\tan\theta_p = \frac{\mu_2}{\mu_1} = \frac{2\sqrt{3}}{2} = \sqrt{3}$$

$$\theta_p = 60^\circ$$

31. Match the list -I with list-II

	List-I		List-II
(A)	Magnetic induction	(I)	$M L T^{-2} A^{-2}$
(B)	Magnetic flues	(II)	$M L^2 T^{-2} A^{-2}$
(C)	Magnetic permeability	(III)	$M L^0 T^{-2} A^{-1}$
(D)	Self induction	(IV)	$M L^2 T^{-2} A^{-1}$

- 1) A – III, B – IV, C – II, D – I                      2) A – I, B – III, C – IV, D – II  
 3) A – IV, B – III, C – I, D – II                      4) A – III, B – IV, C – I, D – II

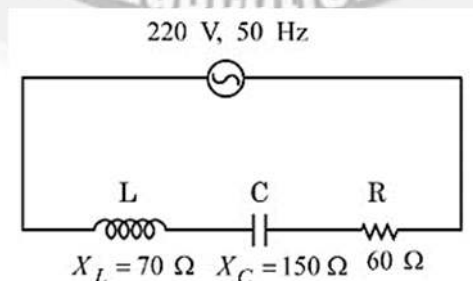
**Key:** 4

**Sol:**  $B = F / m = [mL^0 T^{-2} A^{-1}]$ ,  $\phi = BA = [mL^2 T^{-2} A^{-1}]$

$$\mu_o = \frac{F r^2}{m_1 m_2} = [mL T^{-2} A^{-2}] \quad L = \frac{U}{i^2} = [mL^2 T^2 A^{-2}]$$

32. For a series LCR circuit connected with 220V 50 Hz a.c source as shown in the figure

The power factory is  $\frac{\alpha}{10}$  the value of  $\alpha$  is \_\_\_\_\_



- 1) 10                      2) 4                      3) 6                      4) 8

**Key: 3**

$$\text{Sol: } \cos \phi = \frac{R}{Z} = \frac{R}{\sqrt{(x_c - x_c)^2 + R^2}} = \frac{60}{\sqrt{(150-70)^2 + (60)^2}}$$

$$\cos \phi = \frac{60}{100} = \frac{\alpha}{10}$$

$$\boxed{\alpha = 6}$$

33. Match the list -1 with list-II

	List-I		List-II
A)	Radio wave	I)	Is produced by magnetron value
B)	Micro wave	II)	Due to change in vibrational modes of atoms
C)	Infrared – wave	III)	Due to inner shell electron moving from higher energy level to lower energy level
D)	X-ray	IV)	Due to rapid acceleration of chares

Choose the correct answer from the options given below:

- 1) A → IV, B → I, C → II, D → III      2) A → II, B → IV, C → III, D → I  
 3) A → IV, B → II, C → I, D → III      4) A → IV, B → III, C → I, D → II

**Key: 1**

**Sol:** Radio waves are produced by acceleration of charges, micro waves are produced by magnetron value IR waves are produced by vibration modern of atoms, x rays are produced by electrons moving from high to low

34. A cylindrical block of mass M and area of cross section A is floating in a liquid of density  $\rho$  and with x-axis vertical when depressed a little an released the block starts oscillating the period of oscillation is \_\_\_\_\_

- 1)  $2\pi\sqrt{\frac{A}{Mg}}$       2)  $2\pi\sqrt{\frac{M}{\rho Ag}}$       3)  $\pi\sqrt{\frac{A}{Mg}}$       4)  $\pi\sqrt{\frac{2M}{Ag}}$

**Key: 2****Sol:** In equilibrium

When it is depressed

$$F_{\text{net}} = W_{\text{app}} - F_B(x+y)$$

$$\Rightarrow ma = W_{app} - F_{Bx} - F_{By} \Rightarrow ma = -V_{in} e g$$

$$\Rightarrow ma = -(Ay)e - g \Rightarrow a = -\frac{(Aeg)}{M} y$$

Compare with

$$a = -w^2 y$$

$$\therefore w^2 = \frac{Aeg}{M} \Rightarrow w = \sqrt{\frac{Aeg}{M}}$$

$$T = \frac{2\pi}{\omega} \Rightarrow T = 2\pi \sqrt{\frac{M}{Aeg}}$$

35. Given below are two statements:

**Statement –I :-** For all elements, greater than mass of the nucleus, greater is the binding energy per nucleon

**Statement –II :-** For all elements, nuclei with less binding energy per nucleon transforms to nuclei with greater bonding energy per nucleon

In the light of the above statements, choose the correct answer from the option given below

- 1) Statement –I is true but Statement –II are false
- 2) Both Statement –I and Statement –II are false
- 3) Both Statement –I and Statement –II are true
- 4) Statement –I is false but Statement –II is true

**Key: 4**

**Sol:** Statement-I is false because the binding energy per nucleon generally increases with mass number upto 56 and then it gradually decreases for heavier nuclei

Statement-II is true because less BE/A. nuclei transform into nuclei with greater BE/A

36. The electro static potential in a charged spherical region of radius  $r$  varies as  $V = ar^3 + b$ , where  $a$  and  $b$  are constants. The total charge in the sphere of unit radius is  $\alpha \times \pi \epsilon_0$ . The value of  $\alpha$  is \_\_\_\_\_.

(permittivity of vacuum is  $\epsilon_0$ )

- 1) -8
- 2) -9
- 3) -12
- 4) -6

**Key: 3**

**Sol:** We know  $E = -\frac{dv}{dr} \Rightarrow E = -a(3r^2) + 0 \Rightarrow E = 3ar^2$

From Gauss's law  $\phi = \vec{E} \cdot \vec{ds} = \frac{q}{\epsilon_0} \Rightarrow -3ar^2(4\pi r^2) = \frac{q}{\epsilon_0} \Rightarrow -12\pi ar^4 = \frac{q}{\epsilon_0}$

Given  $r = 1 \Rightarrow q = -12\pi a\epsilon_0$

$\therefore \boxed{\alpha = -12}$

37. Three charges  $+2q, +3q$  and  $-4q$  are situated at  $(0, -3a), (2a, 0)$  and  $(-2a, 0)$  respectively in the  $x$   $y$  plane. The resultant dipole moment about origin is \_\_\_\_\_.

1)  $2qa[3\hat{i} - 7\hat{j}]$       2)  $2qa[3\hat{j} - 7\hat{i}]$       3)  $2qa(7\hat{i} - 3\hat{j})$       4)  $2qa(3\hat{j} - \hat{i})$

**Key: 3**

**Sol:**  $q_1 = +2q$   $r_1 = -3a\hat{j}$

$q_2 = +3q$   $r_2 = 2a\hat{i}$

$q_3 = -4q$   $r_3 = -2a\hat{i}$

$P = \epsilon q r = q_1 r_1 + q_2 r_2 + q_3 r_3$

$P = (2q)(-3a\hat{j}) + 3q(2a)\hat{i} + (-4q)(-2a)\hat{i}$

$P = 2qa[7\hat{i} - 3\hat{j}]$

38. Two resistors of  $100\Omega$  each are connected in series with a  $9V$  battery a voltmeter of  $400\Omega$  resistance is connected to measure the voltage drop across one of the resistances the voltmeter reading is \_\_\_\_\_ V

1) 4.5      2) 4      3) 3      4) 2

**Key: 2**

**Sol:**  $R_{eq} = 100 + 800 = 180$

$I = \frac{9}{180}$

Voltmeter reading =  $iR = \frac{9}{180} \times 80 = 4V$

39. Two masses  $400g$  and  $350g$  are suspended from the ends of a light string passing over a heavy pulley of radius  $2$  cm when released from rest the heavier mass is observed to fall  $81$  cm in  $9s$ . The rotational inertia of the pulley is \_\_\_\_\_  $kg \cdot m^2$ . ( $g = 9.8$   $m/s^2$ )

1)  $4.75 \times 10^{-3}$       2)  $1.86 \times 10^{-2}$       3)  $9.5 \times 10^{-3}$       4)  $8.3 \times 10^{-3}$

**Key: 3**

**Sol:**  $a = \frac{(m_2 - m_1)g}{m_1 + m_2 + \frac{I}{R^2}} \Rightarrow S = 21t + \frac{1}{2}at^2$

$$\frac{81}{100} = 0 + \frac{1}{2} \left[ \frac{m_2 - m_1}{m_1 + m_2 + \frac{I}{R^2}} \right] g (\cancel{g})^2$$

$$\rightarrow \left[ m_1 + m_2 + \frac{I}{R^2} \right] = \frac{1}{2} \frac{(m_2 - m_1)(g)}{100}$$

$$\left[ \frac{750}{1000} + \frac{I}{R^2} \right] = \frac{1}{2} \left[ \frac{50}{1000} \right] (9.8) 100$$

$$\boxed{I = 9.5 \times 10^{-4} \text{ kg m}^2}$$

40. A boy throw's a ball in to air at  $45^\circ$  from the horizontal to land on a roof of a building of height H. If the ball attains maximum height in 2s and land on the building in 3s after launch then the value of H is \_\_\_ m ( $g=10 \text{ m/s}^2$ )

- 1) 15                      2) 20                      3) 10                      4) 25

**Key:** 1

**Sol:**  $t_a = 2 = \frac{u \sin \theta}{g} \quad 2 = \frac{u}{g} \cdot \left( \frac{1}{\sqrt{2}} \right)$

$$u = 2\sqrt{2}g \quad Sg = (u \sin \theta)t - \frac{1}{2}gt^2$$

$$H = 2\sqrt{2}g \left( \frac{1}{\sqrt{2}} \right) (3) - \frac{1}{2}g(3)^2$$

$$\boxed{H = 15\text{m}}$$

41. A brass wire of length 2m and radius 1mm at  $27^\circ\text{C}$  is held taut between two rigid supports initially it was cooled to temperature of  $-43^\circ\text{C}$  creating a tension T in the wire. The temperature to which the wire has to be cooled in order to increase the tension in it to  $1.4T$  is \_\_\_  $^\circ\text{C}$

- 1) -80                      2) -65                      3) -71                      4) -86

**Key:** 3

**Sol:** Thermal stress  $F = yA\alpha \Delta t = yA\alpha [t_2 - t_1]$

$$\frac{T}{1.4T} = \frac{yA\alpha [-43 - 27]}{yA\alpha [t - 27]} \Rightarrow \frac{1}{1.4} = \frac{-70}{t - 27} \Rightarrow t - 27 = -70(1.4) \Rightarrow t = -98 + 27 \Rightarrow \boxed{t = -71^\circ\text{C}}$$

42. Three masses 200 kg, 300 kg and 400 kg are placed at the vertices of an equilateral triangle with sides 20 m. They are rearranged on the vertices of a bigger triangle of side 25 m and with same centre. The work done in this process is \_\_\_ J.

(Gravitational constant  $G = 6.7 \times 10^{-11} \text{ Nm}^2/\text{kg}^2$ )

- 1)  $2.85 \times 10^{-7}$       2)  $4.77 \times 10^{-7}$       3)  $9.86 \times 10^{-6}$       4)  $1.74 \times 10^{-7}$

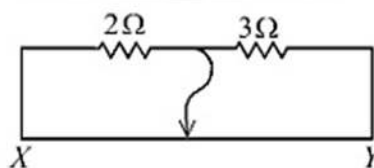
**Key:** 4

**Sol:**  $w = \Delta U$

$$\begin{aligned}
 U_i &= - \left[ \frac{Gm_1m_2}{r_{12}} + \frac{m_2m_3}{r_{23}} + \frac{Gm_3m_1}{r_{13}} \right] \\
 &= - \frac{6.67 \times 10^{-11}}{20} [200 \times 300 + 300 \times 400 + 400 \times 200] \\
 &= - \frac{6.67 \times 10^{11}}{20} [6 + 12 + 8] \times 10^4 \\
 &= - \frac{6.67 \times 10^{-12}}{2} [26] \times 10^4 \\
 &= -86.71 \times 10^{-8} \\
 U_f &= - \frac{6.67 \times 10^{-11}}{25} [26 \times 10^4] \\
 &= -6.93 \times 10^{-7} \\
 &= -69.3 \times 10^{-8} \\
 W &= U_f - U_i = [-69.3 + 86.71] \times 10^{-8} \\
 &= 17.41 \times 10^{-8}
 \end{aligned}$$

$$w = 1.741 \times 10^{-7} \text{ J}$$

43. Two resistors  $2\Omega$  and  $3\Omega$  are connected in the gap of bridge as shown in fig the null point is obtained with the contact of jockey at some point on wire XY. When an unknown resistor is connected in parallel with  $3\Omega$  resistor, the null point is shifted by 22.5cm towards Y. The resistance of unknown resistor is \_\_\_  $\Omega$



- 1) 4      2) 3      3) 1      4) 2

**Key:** 4

**Sol:**  $\frac{P}{Q} = \frac{2}{3}$

$$\frac{2}{3} = \frac{200 - 2}{100 - 2}$$

$$200 - 2 = 3$$

$$200 = 5 \Rightarrow \frac{200}{5} = 40 \text{ cm}$$

If unknown resistor (R) is connected in parallel with  $3\Omega$

$$R, 3 \text{ are in P} \rightarrow \frac{3R}{R+3}$$

$$i = \frac{200}{40 + 22.5} = 40 + 22.5$$

$$= 62.5$$

$$\text{From } \frac{P}{Q} = \frac{i}{100 - i}$$

$$\frac{2(R+3)}{3R} = \frac{62.5}{37.5}$$

$$\frac{2(R+3)}{3R} = \frac{5}{3} \Rightarrow 2R + 3(2) = 5R \Rightarrow 6 = 5R - 2R$$

$$3R = 6$$

$$R = \frac{6}{3} = 2\Omega$$

44. A spring of force constant  $15\text{N/m}$  is cut into two pieces. If the ratio of their lengths is  $1:3$ , then force constant of smaller pieces is \_\_\_  $\text{N/m}$

- 1) 45      2) 15      3) 60      4) 20

**Key:** 3

**Sol:**  $K \propto \frac{1}{l} \Rightarrow K = \text{Constant}$

$$K = k_1 \quad \text{Given } \frac{1}{l_2} = \frac{1}{3l_1} \Rightarrow l_2 = 3l_1$$

$$\text{But } l = l_1 + l_2 = l_1 + 3l_1 = 4l_1 \Rightarrow l_1 = \frac{l}{4}$$

$$\therefore 15 = K_1 \left( \frac{l}{4} \right)$$

$$K_1 = 15 \times 4 \Rightarrow \boxed{K_1 = 60 \text{ N/m}}$$

45. The exit surface of prism with Refractive index  $n$  is coated with material having Refractive index  $n/2$  when this prism is set for minimum angle of deviation. It exactly meets the condition of critical angle, the prism angle is \_\_\_\_\_
- 1)  $15^\circ$                       2)  $60^\circ$                       3)  $45^\circ$                       4)  $30^\circ$

**Key:** 2

**Sol:**  $\sin c = \frac{n/2}{n} = \frac{1}{2}$

At minimum deviation

$$A = 2r = 60^\circ$$

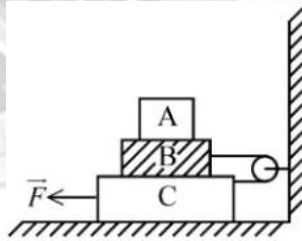
$$r_1 = r_2 = c = 30^\circ$$

### SECTION-II (NUMERICAL VALUE TYPE)

This section contains **5 Numerical Value Type Questions**. The Answer should be within **0 to 9999**. If the Answer is in **Decimal** then round off to the **Nearest Integer** value (Example i.e. If answer is above **10** and less than **10.5** round off is **10** and if answer is from **10.5** and less than **11** round off is **11**).

**Marking scheme: +4 for correct answer, 0 if not attempt and -1 in all other cases**

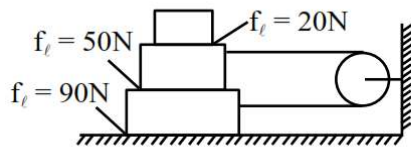
46. In the given figure the blocks A, B and C weigh 4 kg, 6 kg and 8 kg respectively. The coefficient of sliding friction between any two surfaces is 0.5. The force  $F$  required to slide the block C with constant speed is \_\_\_\_\_ N. (Use  $g=10 \text{ m/s}^2$ )



**Key:** 210

**Sol:**

For 8kg to move with constant velocity  $F_{\text{net}} = 0$ .



$$\therefore F = 90 + T + 50 \text{ (for 8kg block)}$$

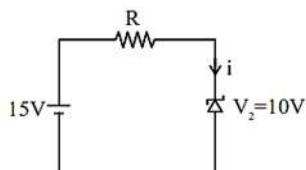
$$T = 20 + 50 \text{ (for 6kg block)}$$

$$\therefore F = 210 \text{ N.}$$

47. A voltage regulating circuit consisting of Zener diode, having break-down voltage of 10 V and maximum power dissipation of 0.4 W, is operated at 15 V. The approximate value of protective resistance in this circuit is \_\_\_\_\_  $\Omega$

**Key:** 125

Sol:



$$P_D = 0.4w = 10i$$

$$i = 0.04A$$

$$R = \frac{15-10}{0.04} = \frac{5}{0.04} = 125 \Omega$$

48. A gas of certain mass filled in a closed cylinder at a pressure of 3.23 kPa has temperature  $50^\circ C$ . The gas is now heated to double its temperature. The modified pressure is \_\_\_\_ Pa.

Key: 3730

$$\text{Sol: } \frac{P_1}{P_2} = \frac{T_1}{T_2} \quad \frac{3.23 \times 10^3}{P_2} = \frac{273+50}{273+100} = \frac{323}{373} \quad P_2 = 3730P$$

49. A short bar magnet placed with its axis at  $30^\circ$  with an external field of 800 Gauss, experiences a torque of 0.016 N.m. The work done in moving it from most stable to most unstable position is  $\alpha \times 10^{-3} J$ . The value of  $\alpha$  is \_\_\_\_

Key: 64

Sol:

$$\tau = \mu B \sin \theta \Rightarrow 0.016 = \mu \times B \times \frac{1}{2}$$

$$\Rightarrow \mu = \frac{0.032}{B}$$

$$W_{\text{ext}} = U_f - U_i = \mu B - (\mu B) = 2\mu B$$

$$= 2 \times \frac{0.032}{B} \times B$$

$$= 0.064 J$$

50. Sixty four rain drops of radius 1 mm each falling down with a terminal velocity of 10 cm/s coalesce to form a bigger drop. The terminal velocity of bigger drop is \_\_\_\_ cm/s.

Key: 160

Sol:

$$V_t = \frac{2r^2g}{9\eta} [\sigma - \rho]$$

$$V_t \propto r^2$$



64 drop

$$64 \left( \frac{4}{3} \pi R_1^3 \right) = \frac{4}{3} \pi R_2^3$$

$$R_2 = 4R_1$$

$$\left( \frac{V_{t1}}{V_{t2}} \right) = \left( \frac{R_1}{R_2} \right)^2 = \left( \frac{1}{4} \right)^2$$

$$\frac{10}{(V_{t2})} = \frac{1}{16}$$

$$(V_{t2}) = 160 \text{ cm/sec}$$

## CHEMISTRY

Max Marks: 100

SECTION-I  
(SINGLE CORRECT ANSWER TYPE)

This section contains **20 Multiple Choice Questions**. Each question has 4 options (1), (2), (3) and (4) for its answer, out of which **ONLY ONE** option can be correct.

**Marking scheme: +4 for correct answer, 0 if not attempted and -1 in all other cases.**

51. Given below are two statements:

**Statement-I:** Hybridisation, shape and spin only magnetic moment of  $K_3[Co(CO_3)_3]$  is  $sp^3d^2$ , octahedral and 4.9 BM respectively.

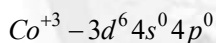
**Statement-II:** Geometry, hybridisation and spin only magnetic moment values (BM) of the ions  $[Ni(CN)_4]^{2-}$ ,  $[MnBr_4]^{2-}$  and  $[CoF_6]^{2-}$  respectively are square planar, tetrahedral, octahedral;  $dsp^2$ ,  $sp^3$ ,  $sp^3d^2$  and 0, 5.9, 4.9.

In light of the above statements, choose the correct answer from the options given below

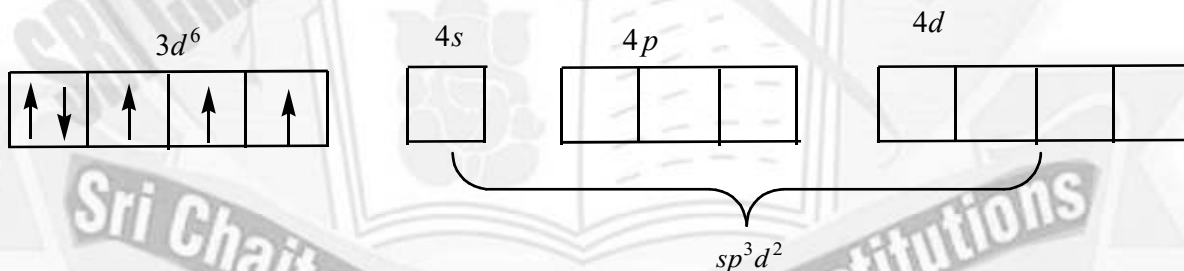
- 1) S-I is true but S-II is false                      2) Both S-I and S-II are true  
3) S-I is false but S-II is true                     4) Both S-I and S-II are false

**Key:** 2

**Sol:** S-I  $K_3[Co(CO_3)_3]$



$Co_3^{2-}$  - Weak field ligand, no pairing of electrons

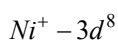


No. of unpaired electrons  $\mu = 4$

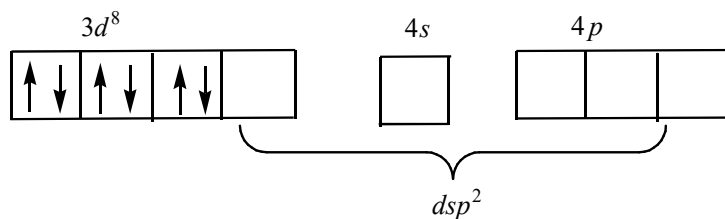
Magnetic moment  $\mu = \sqrt{n(n+2)} BM$

$$\mu = \sqrt{4(4+2)} = \sqrt{24} = 4.9 BM$$

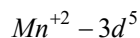
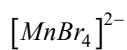
S-II :  $[Ni(CN)_4]^{2-}$



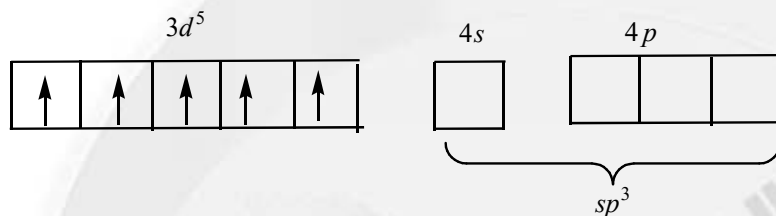
$CN^-$  - strong field ligand, pairing takes place



$$N=0, \mu = 0$$

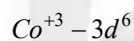
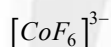


$Br^-$  -weak field ligand, no pairing

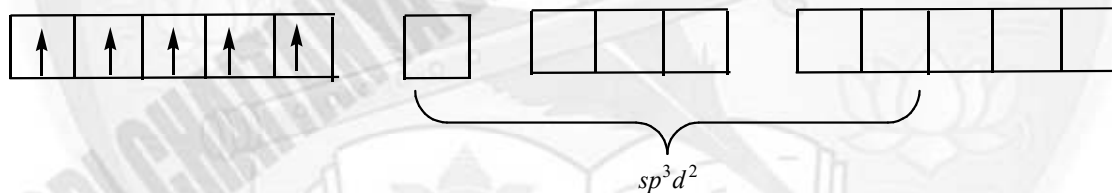


$$n=5$$

$$\mu = \sqrt{5(5+2)} = \sqrt{35} = 5.9 \text{ BM}$$



$F^-$  -weak field ligand, no pairing



$$N=4, \mu = \sqrt{4(4+2)} = \sqrt{24} = 4.9 \text{ BM}$$

52. Given below are statements about some molecules/ions.

Identify the CORRECT statements.

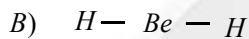
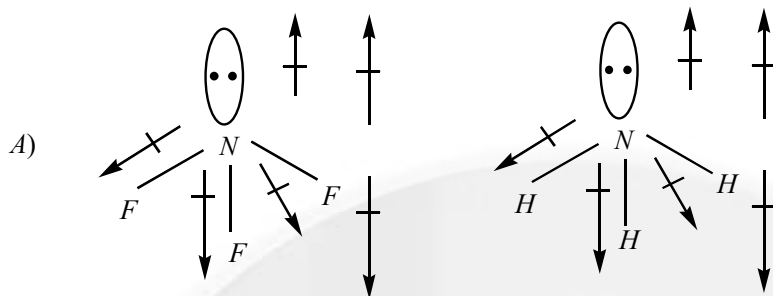
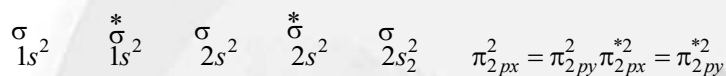
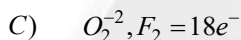
- The dipole moment value of  $NF_3$  is higher than that of  $NH_3$ .
- The dipole moment value of  $BeH_2$  is zero.
- The bond order of  $O_2^{2-}$  and  $F_2$  is same.
- The formal charge on the central oxygen atom of ozone is -1.
- In  $NO_2$ , all the three atoms satisfy the octet rule, hence it is very stable.

Choose the correct answer from the options given below:

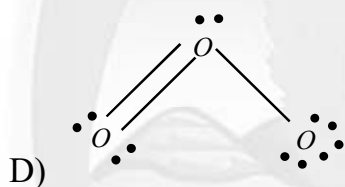
- B & C only
- B, C & D only
- A, C & D only
- A, B, C, D & E

Key:1

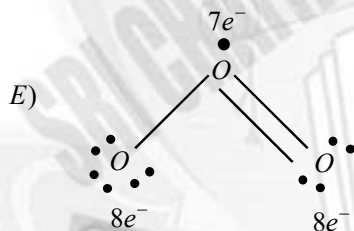
Sol:

Linear  $\mu = 0$ 

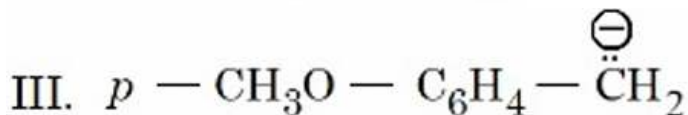
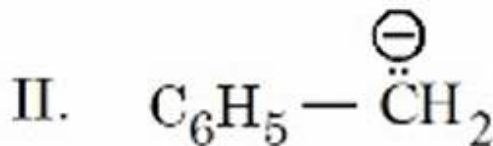
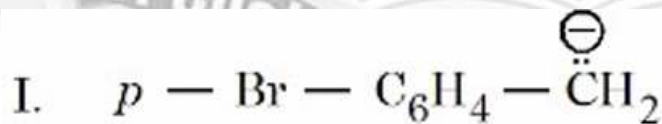
$$B.O. = \frac{1}{2}[N_b - N_a] = \frac{1}{2}[10 - 8] = \frac{2}{2} = 1$$

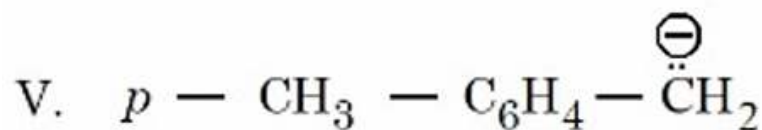
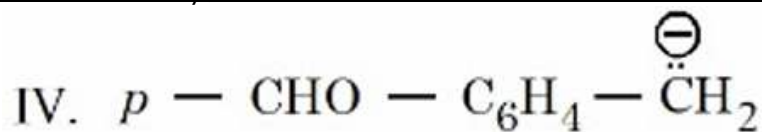


$$\text{Central oxygen} = 6 - 2 - \frac{1}{2}(6) = 6 - 5 = +1$$



53. Arrange the following combinations in the decreasing order of stability



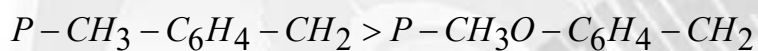
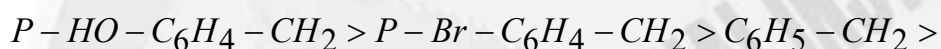


Choose the correct answer from the options given below:

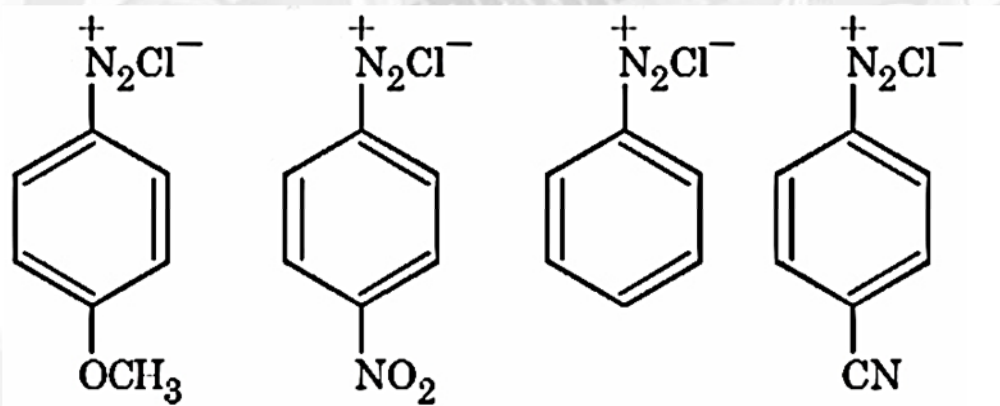
- 1) IV > II > I > III > V                      2) I > IV > II > V > III  
 3) I > II > IV > V > III                      4) IV > I > II > V > III

**Key:** 4

**Sol:** Stability of carbanion directly proportional to -j groups (E.W.G)



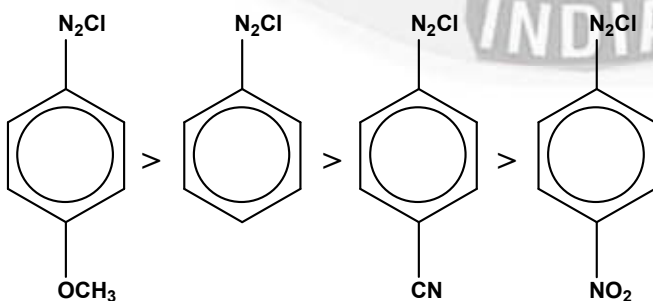
54. The correct stability order of the following diazonium salts is



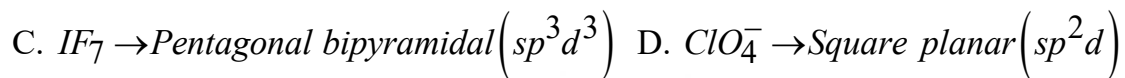
- 1) C > A > D > B                      2) A > B > C > D  
 3) A > C > D > B                      4) C > D > B > A

**Key:** 3

**Sol:** Diazonium salt stabilized by E.D.G.



55. Among the following, the correct combinations are



Choose the correct answer from the options given below:

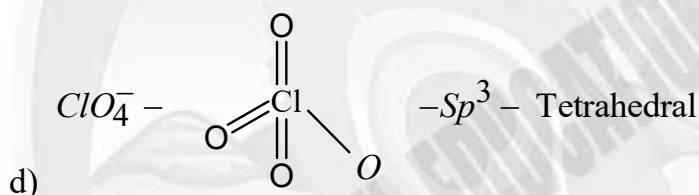
- 1) A, B and C only                                      2) A and B only  
3) A, B, C and D                                      4) B, C and D only

**Key:** 1

**Sol:** A)  $IF_3 - AB_3E_2$  type - T-shape -  $Sp^3d$

B)  $IF_5 - AB_5E$  type - Square pyramidal -  $Sp^3d^2$

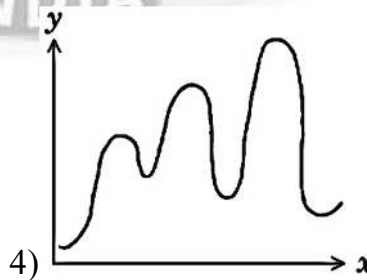
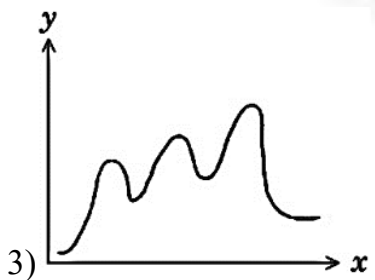
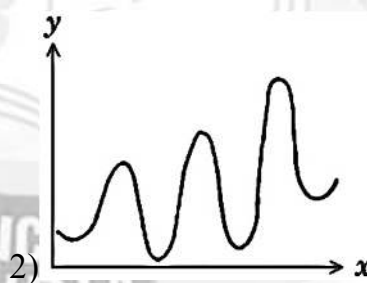
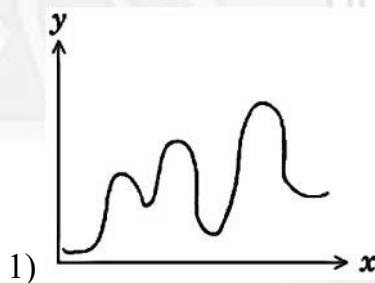
C)  $IF_7 - AB_7$  type - Pentagonal bipyramidal ( $Sp^3d^3$ )



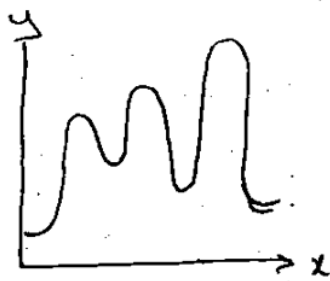
56.  $A \rightarrow D$  is an endothermic reaction occurring in three steps (elementary).



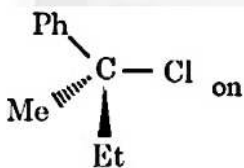
Which of the following graphs between potential energy (y-axis) vs reaction coordinate (x-axis) correctly represents the reaction profile of  $A \rightarrow D$ ?



Key: 4

Sol:  $A \rightarrow D$        $\Delta H = +ve$      $\Delta H = H_P - H_R (H_P > H_R)$ (i)  $A \rightarrow B$        $\Delta H_i = +ve$     ( $H_P > H_R$ )(ii)  $B \rightarrow C$        $\Delta H_{ii} = -ve$     ( $H_P < H_R$ )(iii)  $C \rightarrow D$        $\Delta H_{iii} = -ve$     ( $H_P < H_R$ )

57. Given below are two statements

**Statement-I:** 'C - Cl' bond is strong in  $CH_2 = CH - Cl$  than  $CH_3 - CH_2 - Cl$ **Statement-II:** The given optically active molecule,

hydrolysis gives a solution that can rotate the plane polarized light.

In the light of the above statements, choose the correct answer from the options given below.

- 1) S-I is true but S-II is false      2) Both S-I and S-II are false  
 3) Both S-I and S-II are true      4) S-I is false but S-II is true

Key: 3

Sol: Conceptual

58. Match List-I with List-II

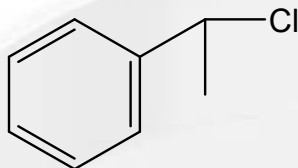
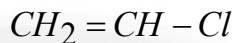
List-I Chloro derivative		List-II Example	
A.	Vinyl Chloride	I.	$CH_2 = CH - CH_2Cl$
B.	Benzyl Chloride	II.	$CH_3 - CH(Cl)CH_3$
C.	Alkyl Chloride	III.	$CH_2 = CHCl$
D.	Allyl Chloride	IV.	

Choose the correct answer from the options given below:

- 1) A-III, B-IV, C-I, D-II                      2) A-IV, B-I, C-III, D-II  
 3) A-I, B-II, C-IV, D-III                      4) A-III, B-IV, C-II, D-I

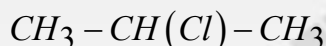
**Key:** 4

**Sol:** Vinyl chloride

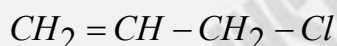


Benzyl chloride

Alkyl chloride



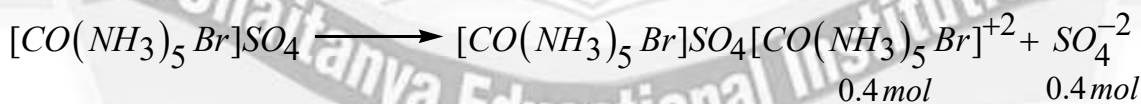
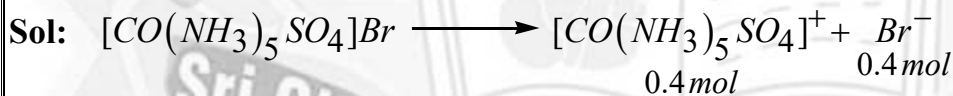
Allyl chloride



59. Consider a mixture 'X' which is made by dissolving 0.4 mol of  $[Co(NH_3)_5SO_4]Br$  and 0.4 mol of  $[Co(NH_3)_5Br]SO_4$  in water to make 4 L of solution. When 2 L of mixture 'X' is allowed to react with excess of  $AgNO_3$ , it forms precipitate 'Y'. The rest 2 L of mixture 'X' reacts with excess  $BaCl_2$  to form precipitate 'Z'. which of the following statements is CORRECT?

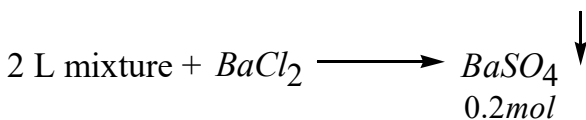
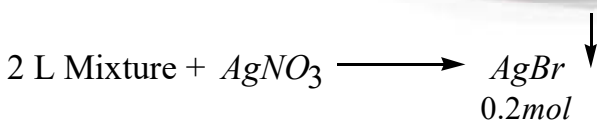
- 1) 0.1 mol of 'Y' is formed                      2) 0.2 mol of 'Z' is formed  
 3) 0.4 mol of 'Z' is formed                      4) 'Y' is  $BaSO_4$  and 'Z' is  $AgBr$

**Key:** 2



X & Y mixed in 4 L

2 L solution contain 0.2 mol  $Br^-$  & 0.2 mol  $SO_4^{-2}$



60. Consider three metal chlorides x, y and z, where x is water soluble at room temperature, y is sparingly soluble in water at room temperature and z is soluble in hot water. x, y and z are respectively

- 1)  $MgCl_2$ ,  $AgCl$  and  $AlCl_3$                       2)  $CuCl_2$ ,  $AgCl$  and  $PbCl_2$   
 3)  $AgCl$ ,  $Hg_2Cl_2$  and  $PbCl_2$                       4)  $AlCl_3$ ,  $PbCl_2$  and  $BaCl_2$

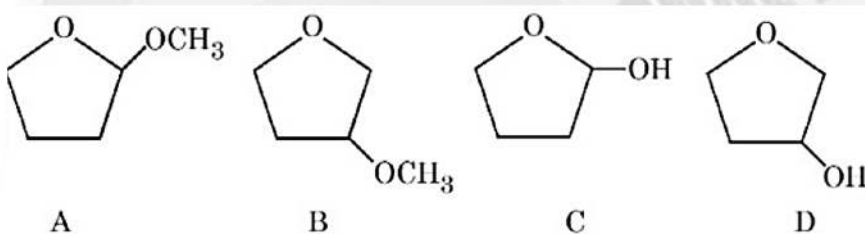
**Key:** 2

**Sol:**  $X = CuCl_2$  soluble in water at room temperature

$Y = AgCl$  sparingly soluble in water at room temperature.

$Z = PbCl_2$  soluble in hot water.

61. A student is given one compound among the following compounds that gives positive test with Tollen's reagent.

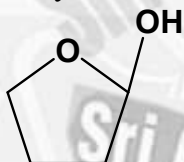


The compound is

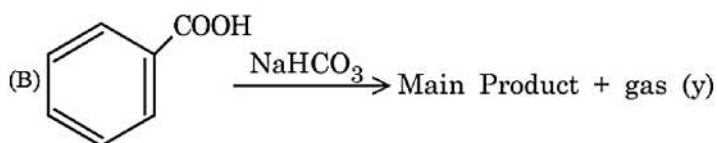
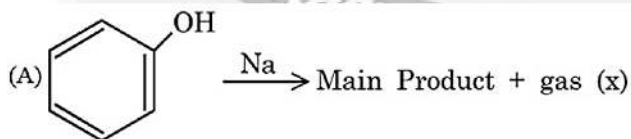
- 1) A                      2) D                      3) C                      4) B

**Key:** 3

**Sol:** Only hemiacetals give Tollen's test



62. Consider the following two reactions A and B

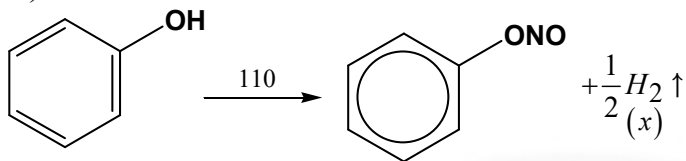


Numerical value of [molar mass of x + molar mass of y] is ...

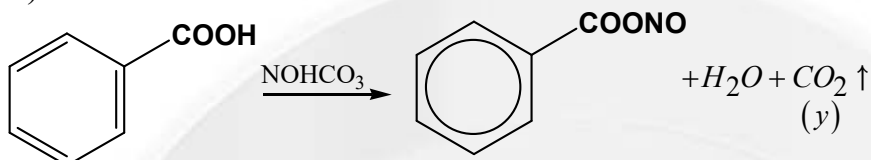
- 1) 4                      2) 46                      3) 88                      4) 160

Key: 2

Sol: A)



B)

Molar mass of  $\text{H}_2(x) = 2$ Molar mass of  $\text{CO}_2(y) = 44$ 

$$x + y = 46$$

63. Given below are two statements;

**Statement-I:** The number of paramagnetic species among
 $[\text{CoF}_6]^{3-}$ ,  $[\text{TiF}_6]^{3-}$ ,  $\text{V}_2\text{O}_5$  and  $[\text{Fe}(\text{CN})_6]^{3-}$  is 3.
**Statement-II:**
 $K_4[\text{Fe}(\text{CN})_6] < K_3[\text{Fe}(\text{CN})_6] < [\text{Fe}(\text{H}_2\text{O})_6]\text{SO}_4 \cdot \text{H}_2\text{O} < [\text{Fe}(\text{H}_2\text{O})_6]\text{Cl}_3$ 

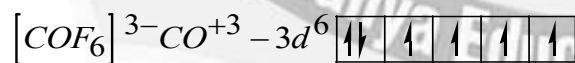
$[\text{Fe}(\text{H}_2\text{O})_6]\text{Cl}_3$  is the correct order in terms of number of unpaired element(s) present in the complexes.

In the light of the above statements, choose the correct answer from the options given below

- 1) Both S-I and S-II are true                      2) S-I is false but S-II is true  
 3) S-I is true but S-II is false                    4) Both S-I and S-II are false

Key: 1

Sol: S-I



$\text{F}^-$  - weak field ligand, no pairing.

No. of unpaired  $e^-s(n) = 4$

$\therefore$  Paramagnetic



66. The hydroxy compound (X) with molar mass  $122 \text{ g mol}^{-1}$  is acetylated with acetic anhydride, using a large excess of the reagent ensuring complete acetylation of all hydroxyl groups. The product obtained has a molar mass of  $290 \text{ g mol}^{-1}$ . The number of hydroxyl groups present in compound (X) is:

- 1) 4                      2) 3                      3) 2                      4) 5

**Key:** 1

**Sol:** No. of hydroxyl groups =  $\frac{\text{molar mass of acetylated product} - \text{molar mass of original compound}}{42}$

$$= \frac{290 - 122}{42} = \frac{168}{42} = 4$$

67. At  $27^\circ\text{C}$  in presence of a catalyst, activation energy of a reaction is lowered by  $10 \text{ kJ mol}^{-1}$ . The logarithm of ratio of  $\frac{k(\text{catalysed})}{k(\text{uncatalysed})}$  is ....

(Consider that the frequency factor for both reactions is same)

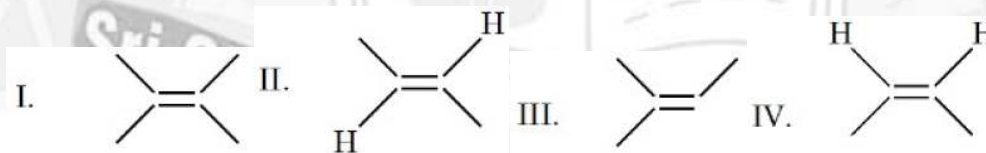
- 1) 3.482                      2) 1.741                      3) 17.41                      4) 0.1741

**Key:** 2

**Sol:**  $\frac{K_{\text{catalyst}}}{K_{\text{uncatalyst}}} = e^{-E_a/RT}$

$$\log \frac{K_c}{K_u} = \frac{\Delta E}{2.303RT} = \frac{10 \times 1000}{2.303 \times 8.314 \times 300} = 1.741$$

68. Arrange the following alkenes in decreasing order of stability

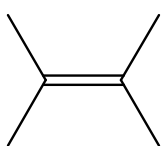


Choose the correct answer from the options given below:

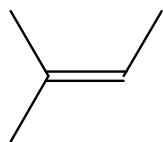
- 1) I > III > II > IV    2) III > II > I > IV  
3) I > III > IV > II    4) III > I > II > IV

**Key:** 1

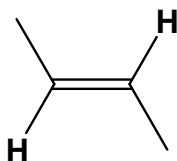
**Sol:** More substituted alkeny are more stable by hyper conjugation



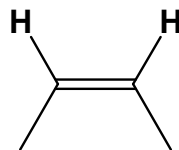
I



III



II



IV

69. 'W' g of non-volatile electrolyte solid solute of molar mass 'M' g mol<sup>-1</sup> when dissolved in 100 mL water, decreases vapour pressure of water from 640mm Hg to 600 mm Hg. If aqueous solution of the electrolyte boils at 375 K and K<sub>b</sub> for water is 0.52 K kg mol<sup>-1</sup>, then the mole fraction of the electrolyte solution (x<sub>2</sub>) in the solution can be expressed as ( Given: Density of water = 1 g/mL and boiling point of water = 373 K)

1)  $\frac{16}{2.6} \times \frac{W}{M}$       2)  $\frac{1.3}{8} \times \frac{M}{W}$       3)  $\frac{2.6}{16} \times \frac{M}{W}$       4)  $\frac{1.3}{8} \times \frac{W}{M}$

**Key:** 4

**Sol:**  $\Delta T_b = i K_b m$

$$2 = i \times 0.52 \times \frac{\frac{w}{100}}{1000}$$

$$i \times \frac{w}{m} = 2 \times \frac{100}{1000} \times \frac{1}{52}$$

$$i = \frac{1}{2.6} \times \frac{m}{w}$$

$$RLVP = \frac{P^0 - P_s}{P^0} = i \times X_{solute}$$

$$\frac{640 - 600}{640} = i \times X_{solute}$$

$$\frac{1w}{16} = \frac{1}{2.6} \times \frac{m}{w} \times X_{solute}$$

$$X_{solute} = \frac{1.3}{8} \times \frac{w}{m}$$

70. Match List-I with List-II

List-I Isothermal process for ideal gas system		List-II Work done ( $V_f > V_i$ )	
A.	Reversible expansion	I.	$w = 0$
B.	Free expansion	II.	$w = -nRT \ln \frac{V_f}{V_i}$
C.	Irreversible expansion	III.	$w = -P_{ex} (V_f - V_i)$
D.	Irreversible compression	IV.	$w = -P_{ex} (V_i - V_f)$

Choose the correct answer from the options given below:

- 1) A-IV, B-II, C-III, D-I                      2) A-II, B-I, C-III, D-IV  
 3) A-I, B-III, C-II, D-IV                      4) A-IV, B-I, C-III, D-II

**Key:** 2**Sol:** Reversible expansion

$$w = -nRT \ln \frac{V_f}{V_i}$$

Free expansion  $w = 0$ 

Irreversible expansion

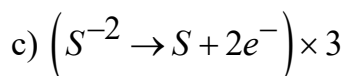
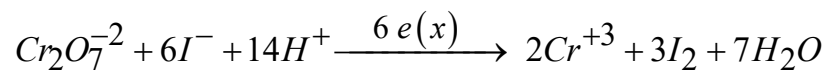
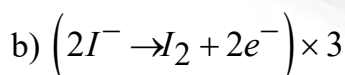
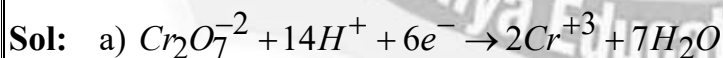
$$w = -P_{ex} (V_f - V_i)$$

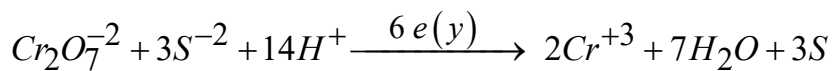
Irreversible compression

$$w = -P_{ex} (V_i - V_f)$$

**Section-II****(NUMERICAL VALUE Type**

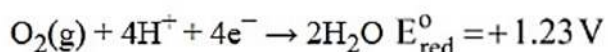
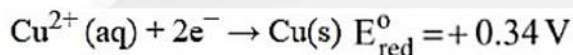
This section contains 5 Numerical Value Type Questions. The Answer should be within 0 to 9999. If the Answer is in Decimal then round off to the Nearest Integer value (Example i.e. If answer is above 10 and less than 10.5 round off is 10 and if answer is from 10.5 and less than 11 round off is 11).

**Marking scheme: +4 for correct answer, 0 if not attempt and -1 in all other cases**71. X and Y are the number of electrons involved, respectively during the oxidation of  $I^-$  to  $I_2$  and  $S^{2-}$  to S by acidified  $K_2Cr_2O_7$ . The value of X + Y is \_\_\_\_\_.**Key:** 12



$$x + y = 6 + 6 = 12$$

72. Electricity is passed through an acidic solution of  $\text{Cu}^{2+}$  till all the  $\text{Cu}^{2+}$  was exhausted, leading to the deposition of 300 mg of Cu metal. However, a current of 600 mA was continued to pass through the same solution for another 28 minutes by keeping the total volume of the solution fixed at 200 mL. The total volume of oxygen evolved at STP during the entire process is \_\_\_ mL. (nearest integer)



$$\text{Molar mass of Cu} = 63.54 \text{ g mol}^{-1}$$

$$\text{Molar mass of O}_2 = 32 \text{ g mol}^{-1}$$

$$\text{Faraday Constant} = 96500 \text{ C mol}^{-1}$$

$$\text{Molar volume at STP} = 22.4 \text{ L}$$

**Key:** 111

**Sol:** Equation of Cu = Equation of  $\text{O}_2$

$$\frac{300 \times 10^{-3} \times 2}{63.54} = n_{\text{O}_2} \times 4$$

$$n_{\text{O}_2} = 2.36 \times 10^{-3}$$

$$\text{When current is further passed } n_{\text{O}_2} \times 4 = \frac{600 \times 28 \times 60}{96500 \times 1000}$$

$$n_{\text{O}_2} = 2.611 \times 10^{-3}$$

$$\text{Total O}_2 \text{ released} = \left[ 10^{-3} \times (2.36 + 2.611) \right] \times 22400 = 111.35 \text{ ml}$$

73. Consider two group IV metal ions  $\text{X}^{2+}$  and  $\text{Y}^{2+}$

A solution containing 0.01 M  $\text{X}^{2+}$  and 0.01 M  $\text{Y}^{2+}$  is saturated with  $\text{H}_2\text{S}$ . The pH at which the metal sulphide YS will form as a precipitate is ... (nearest integer)

(Given:  $K_{sp}(XS) = 1 \times 10^{-22}$  at  $25^\circ\text{C}$ ,  $K_{sp}(YS) = 4 \times 10^{-16}$  at  $25^\circ\text{C}$ ,  
 $[\text{H}_2\text{S}] = 0.1\text{M}$  in solution,  $K_{a1} \times K_{a2}(\text{H}_2\text{S}) = 1.0 \times 10^{-21}$ ,  $\log 2 = 0.30$ ,  
 $\log 3 = 0.48$ ,  $\log 5 = 0.70$ )

**Key:** 4

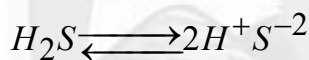
**Sol:** ppt of YS begins when I.P. of  $(Y^{+2})(S^{-2}) > K_{SP}$  of YS

$$[Y^{+2}] = 0.01\text{M} \ \& \ K_{SP}(YS) = 4 \times 10^{-16}$$

min sulphide ion conc. Required

$$[S^{-2}]_{\min} = \frac{K_{SP}(YS)}{[Y^{+2}]} = \frac{4 \times 10^{-16}}{10^{-2}} = 4 \times 10^{-14}$$

For the dissociation of  $\text{H}_2\text{S}$  in solution. The overall equation constant  $K_a, K_{a2}$  is given by



$$K_{a1} \cdot K_{a2} = \frac{[H^+]^2 [S^{-2}]}{[H_2S]}$$

$$K_{a1} \cdot K_{a2} = 1 \times 10^{-21} \ \& \ [H_2S] = 0.1\text{M}$$

$$[H^+]^2 = \frac{K_{a1} \cdot K_{a2} [H_2S]}{[S^{-2}]} = \frac{1 \times 10^{-21} \times 10^{-1}}{4 \times 10^{-14}}$$

$$[H^+] = 0.5 \times 10^{-4}\text{M} \quad pH = 4.3$$

74. The hydrogen spectrum consists of several spectral lines in Lyman series ( $L_1, L_2, L_3, \dots$ ;  $L_1$  has lowest energy among Lyman series). Similarly it consists of several spectral lines in Balmer series ( $B_1, B_2, B_3, \dots$ ;  $B_1$  has lowest energy among Balmer lines). The energy of  $L_1$  is  $x$  times the energy of  $B_1$ . The value of  $x$  is ...  $\times 10^{-1}$  (Nearest integer)

**Key:** 54

$$\text{Sol: } \Delta E_L = 13.6 \times Z^2 \left[ \frac{1}{1^2} - \frac{1}{2^2} \right] = 13.6 \times Z^2 \times \frac{3}{4}$$

$$\Delta E_B = 13.6 \times Z^2 \left[ \frac{1}{2^2} - \frac{1}{3^2} \right] = 13.6 \times Z^2 \times \frac{5}{4 \times 9}$$

$$\frac{\Delta E_L}{\Delta E_B} = \frac{3}{5} \times 9 = \frac{27}{5} = 5.4 = 54 \times 10^{-1}$$

$$\therefore x = 54$$

75. In Dumas method for estimation of nitrogen, 0.50 g of an organic compound gave 70 mL of nitrogen collected at 300 K and 715 mm pressure. The percentage of nitrogen in the organic compound is ....% (Aqueous tension at 300 K is 15 mm).

**Key:** 15

$$\text{Sol: } \%N = \frac{28}{22400} \times \frac{\text{vol. no. } N_2 \text{ at STP}}{\text{wt of O.C.}} \times 100$$

$$= \frac{28}{22400} \times \frac{69.16}{0.5} \times 100$$

$$= 14.65\%$$

$$\approx 15$$

STP given

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

$$\frac{760 \times 70}{300} = \frac{(715 - 15) V_2}{273}$$

$$V_2 = \frac{760 \times 70}{300} \times \frac{273}{700} = 69.16$$



**TOPPERS ARE NOT BORN, THEY'RE MADE @ SRI CHAITANYA**

**SEIZES 3 RANKS IN TOP 10 IN JEE MAIN 2025 (ALL-INDIA OPEN CATEGORY)**



**1**  
ALL INDIA RANK  
OPEN CATEGORY  
Ajay Reddy Vangaia  
Appl. No. 250310265693  
Classroom Student from Grade 11-12B



**1**  
ALL INDIA RANK  
OPEN CATEGORY  
Devclutta Majhi  
Appl. No. 25030018185\*



**10**  
All India Rank Open Category  
**295**  
300 Marks  
Saksham Jindal  
Appl. No. 250310236696\*

**Secured 31 ranks in Top 100 All INDIA Open Category**

 <b>12</b> RANK SAURAV Appl. No. 250310254344*	 <b>22</b> RANK LAKSHYA SHARMA Appl. No. 250310034153*	 <b>31</b> RANK BANDARI RUSHMITH Appl. No. 250310395238	 <b>32</b> RANK BHAVESH JAYANTHI Appl. No. 250310259939	 <b>33</b> RANK UJJWAL KESARI Appl. No. 250310088860*	 <b>36</b> RANK PRADISH GANDHI S Appl. No. 250310788252*
 <b>39</b> RANK S SAI RISHANTH REDDY Appl. No. 250310583519	 <b>41</b> RANK PRASANNA KS Appl. No. 250310328857	 <b>43</b> RANK KOLLI BOINA MUNI SAI Appl. No. 250310480635	 <b>44</b> RANK GORRE NITHIN REDDY Appl. No. 250310551436	 <b>53</b> RANK U RAMA CHARAN REDDY Appl. No. 250310280782	 <b>56</b> RANK ARNAV NIGAM Appl. No. 250310126446
 <b>60</b> RANK SAM UDRA SARKAR Appl. No. 250310179442*	 <b>61</b> RANK SOHAN KALIDAS CHELEKAR Appl. No. 250310202114*	 <b>64</b> RANK BUDUMURU VIKRAM RAJA Appl. No. 250310324700	 <b>66</b> RANK SHAGANTI THRISHUL Appl. No. 250310500006	 <b>70</b> RANK LAXIBHARGAV MENDE Appl. No. 250310248090	 <b>71</b> RANK D CHETAN RAO Appl. No. 250310535984
 <b>73</b> RANK VPRAVAS REDDY Appl. No. 250310253376	 <b>75</b> RANK P SAI SURYA KARTHIK Appl. No. 250310407661	 <b>76</b> RANK YASH KUMAR Appl. No. 250310204405*	 <b>81</b> RANK P PRANAYA SAI MUKESH Appl. No. 250310808114	 <b>89</b> RANK ADITYA SINGH Appl. No. 250310151728	 <b>91</b> RANK JAY A GARWAL Appl. No. 250310122371*
 <b>94</b> RANK V ESWAR KARTHIK Appl. No. 250310233425	 <b>96</b> RANK SAKSHAM GARG Appl. No. 250310026725*	 <b>97</b> RANK RANVEER SINGH VIRDE Appl. No. 250310790734			

BELOW 100 ALL INDIA OPEN CATEGORY RANKS

**31**

BELOW 500 ALL INDIA OPEN CATEGORY RANKS

**95**

BELOW 10 ALL INDIA OPEN CATEGORY RANKS

**10**

BELOW 100 ALL INDIA OPEN CATEGORY RANKS

**98**

BELOW 1000 ALL INDIA OPEN CATEGORY RANKS

**579**

TOTAL QUALIFIED RANKS FOR JEE ADVANCED-2025

**22,094**



**LEADING BY MILES SRI CHAITANYA DOMINATES**  
**JEE ADVANCED 2025**

**29 Ranks in Top 100 in All-India Open Category**



**4 Students in Top 11 in JEE-Advanced 2025, All India Open Category**

<b>16</b> RANK  DEV DUTTA MAJHI HT. No. 255053116*	<b>18</b> RANK  DHARMANA GNANA RUTVIK SAI HT. No. 256056278	<b>19</b> RANK  VANGALA AJAY REDDY HT. No. 256131009	<b>23</b> RANK  AKSH GOGI HT. No. 252071075*	<b>26</b> RANK  P HEMA SAI SURYA KARTHIK HT. No. 256033006	<b>27</b> RANK  SARKARSAMUDRA HT. No. 252071105*
<b>30</b> RANK  OM PRAKASH BEHERA HT. No. 252021018*	<b>32</b> RANK  SUNKARA SAI RISHANTH REDDY HT. No. 256165327	<b>34</b> RANK  DHRUBA JYOTHI PANJA HT. No. 252048248*	<b>35</b> RANK  BHAVESH JAYANTHI HT. No. 251043080	<b>36</b> RANK  ADVAY MAYANK HT. No. 252104113*	<b>37</b> RANK  KARMANYA GUPTA HT. No. 252081477*
<b>42</b> RANK  MD ANAS HT. No. 252046210*	<b>45</b> RANK  RAMIT GOYAL HT. No. 257001113*	<b>52</b> RANK  MAULIK JAIN HT. No. 252079407*	<b>54</b> RANK  GARV HT. No. 252056188*	<b>59</b> RANK  LARISSA HT. No. 252079071*	<b>60</b> RANK  ARYAN BALABADRULA HT. No. 256132077
<b>63</b> RANK  SAMYAJYOTI BISWAS HT. No. 255058456*	<b>64</b> RANK  AARUSH AHAD HT. No. 251036116*	<b>72</b> RANK  RUSHMITH BANDARI HT. No. 259188046	<b>78</b> RANK  KORIKANA RASAGNYA HT. No. 256057046	<b>87</b> RANK  LAKSHYA SHARMA HT. No. 252070075*	<b>91</b> RANK  AVANEESH BANSAL HT. No. 251113138*
<b>95</b> RANK  KAVYA AGGARWAL HT. No. 252072121*					

BELOW 100 ALL INDIA OPEN CATEGORY RANKS > **29** | BELOW 500 ALL INDIA OPEN CATEGORY RANKS > **113** | BELOW 1000 ALL INDIA OPEN CATEGORY RANKS > **205** | BELOW 1000 ALL INDIA CATEGORY RANKS COUNT > **745** | NUMBER OF QUALIFIED RANKS **4,212**